Benchmark Models for the Analysis and Control of Small-Signal Oscillatory Dynamics in Power Systems

IEEE Task Force on Benchmark Systems for Stability Controls

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¹**Abstract**—This paper summarizes a set of six benchmark systems for the analysis and control of electromechanical oscillations in power systems recommended by the IEEE Task Force on Benchmark Systems for Stability Controls of the Power System Dynamic Performance Committee. The benchmark systems were chosen for their tutorial value and particular characteristics leading to control system design problems relevant to the research community. For each benchmark, the modelling guidelines are provided, along with eigenvalues and time-domain results produced with at least two simulation software, and one possible control approach is provided for each system as well. Researchers and practicing engineers are encouraged to use these benchmark systems when assessing new oscillation damping control strategies.

Index terms— benchmark system, small-signal stability, electromechanical oscillations, damping controller, power system stabilizer.

I. INTRODUCTION

A major root cause of large-scale power system blackouts is poorly-damped or unstable electromechanical oscillations which are inherent to interconnected power systems [1]. Therefore, reliable planning and operation of power systems to ensure satisfactory damping performance is of considerable practical interest. Indeed, due to a number of factors including the increasing size, dynamic complexity and utilization of power systems provision of adequate damping remains an important research challenge [2], [3], [4]. In this context, the paper summarizes the set of six carefully chosen benchmark power system models as recommended by the IEEE Task Force (TF) on Benchmark Systems for Stability Controls established by the Power System Stability Controls Subcommittee of the Power System Dynamic Performance Committee [5]. A ‘benchmark system’ comprises a model of the power system together with a set of conventional Power System Stabilizers (PSSs) whose parameters are soundly tuned

in accordance with one of several techniques that are widely applied in practice. Thus, these benchmark systems provide a basis for assessing the damping performance of novel damping controls and/or tuning methodologies to the research community.

Installing power system stabilizers (PSSs) to increase the damping component of the electrical torque of a synchronous generator through the modulation of its excitation voltage, has been the industry practice for many decades to improve the small-signal stability of interconnected power systems [6]. Many variants of the phase compensation designs of the 1970s have been proposed to minimize possible adverse dynamic effects of this controller at non-electromechanical frequencies [2], [7]. The advances in robust control theory over the years have also led to a number of alternative PSSs, all acting through the automatic voltage regulator (AVR) and exciter of the synchronous machines [8], [9], [10]. Controllers with structures other than the lead-lag phase compensation and/or applied to FACTS devices have been termed Power Oscillation Dampers (PODs) [11].

Many methods to tune the parameters of conventional PSSs and PODs have been proposed and continue to appear in the literature. The performance of the new controller is usually verified by digital simulations and compared to that of a conventional PSS using a test system built mainly to highlight the advantages of the new controller. In such cases there is a tendency to over-emphasize the benefits of the new controller in comparison with well applied conventional solutions. Thus, there is a clear need for a set of benchmark systems with soundly tuned conventional PSSs to provide a common basis for fairly evaluating the performance of novel damping controllers and/or PSS tuning methods in comparison with conventional approaches.

The prime objectives of the TF on Benchmark Systems are:

- Select a set of power system models that has tutorial value and present challenges from the perspective of small-signal stability analysis and control.
- Propose at least one possible conventional damping control approach for each system model based on common industry practices.
- Implement the system models and their respective damping control solutions in at least two simulation software packages that have the capability of performing eigena-

¹ This paper has been prepared by the contributors of the IEEE Task Force (TF) on Benchmark Systems for Stability Controls, Power System Stability Controls Subcommittee, Power System Dynamic Performance Committee. The list of authors on top of the paper is organized in alphabetical order.

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analysis and time-domain simulations.

- Validate the benchmark models by confirming (i) that the damping performance of the system with the proposed damping controllers is satisfactory; and (ii) there is close agreement between the results obtained with the respective simulation packages.

As mentioned earlier, each selected system model along with its proposed conventional damping control solution is referred to as a benchmark system.

The criteria used for selecting the benchmark systems are outlined in Section II, while Section III presents the proposed damping control solutions for all the benchmark systems. Section IV describes the procedure used for implementing and validating the benchmark systems, and Section V summarizes the paper.

II. THE BENCHMARK SYSTEMS AND THEIR SELECTION CRITERIA

SMIB test systems have been extensively used for the study of electromechanical oscillations [12]. The SMIB model effectively considers many of the practical aspects related to the field commissioning and testing of stabilizers, in which it is usually not possible to excite inter-area modes [13]. However, the simplifications inherent to the SMIB model hinders its applicability to the study of system-wide (inter-area) oscillations in large interconnected power systems [2]. Other important aspects that may require a detailed multi-machine power system representation include: (i) the coordination of multiple controllers to simultaneously damp several modes; and (ii) robust damping of electromechanical modes for a range of operating conditions.

The following requirements were considered for the selection of a power system model as a benchmark system:

- The system must have multiple machines and exhibit a combination of local and inter-area modes. Other types of modes (e.g., intra-plant modes) can also be present to better reflect practical system conditions. One or more of the electromechanical modes must be poorly damped without damping controls.
- The system must be provided with at least one soundly implemented conventional damping control approach whose action results in satisfactory damping performance.
- Consistent with the TF objectives the system must have been validated by comparing its eigenvalues and non-linear time-domain responses from at least two different simulation software packages.

The addition of a stabilizer to a system under expansion is usually made in coordination with the previously existing stabilizers, and the simultaneous design of several stabilizers is rarely required in practice. Therefore, approaches comprising the design of just a few stabilizers were proposed for the benchmarks since these are of more practical interest.

The selected benchmarks are small-scale test systems that are simple and easy to handle, while still maintaining the characteristics of interest. Most of the benchmark systems do not assess the performance of the stabilizers with respect to

changes in the system operating condition or to nonlinear behavior due to large disturbances. Such assessments are, of course, necessary in practice.

Based on the aforementioned criteria, six systems were chosen, each focusing on an issue of practical interest to oscillation damping. During model validation sometimes unavoidable discrepancies between the results from the different simulators (due to different built-in models offered by different software, for example) were highlighted and their probable source discussed where appropriate.

The main characteristics of the six benchmark systems are briefly described in Table 1. Results from the validation activities, as well as the complete set of data for each of the benchmark systems, can be found in [5] or, alternatively, retrieved from the TF website which can be accessed in ewh.ieee.org/soc/pes/psdpc/PSDP_benchmark_systems.htm.

However, it is worth emphasizing that the TF does not recommend or endorse the use of a specific model or any particular simulation software to perform the linear analyses or the nonlinear simulations in order to reproduce the reported results. For the analysis of a particular benchmark, the TF recommendation is to use a software that produces results close to those reported herein and in [5].

Table 1- Summary of the benchmark systems

System	Buses	Gens	Damping Control Issue
1	6	3	Simultaneous damping of intra-plant, local (inter-plant) and inter-area modes
2	7	5	Poor controllability due to zeroes in the vicinity of the critical electromechanical mode
3	11	4	Simultaneous damping of local and inter-area modes in a highly symmetrical system
4	39	10	Coordination of multiple stabilizers to damp electromechanical modes within a control area
5	59	14	Simultaneous damping of local and inter-area modes, small- and large-disturbance analysis of a system for multiple operating conditions.
6	68	16	Coordination of multiple stabilizers to damp multiple local and inter-area modes

III. DESCRIPTION OF THE BENCHMARK SYSTEMS

This section describes the structure and the electromechanical oscillation problem posed by each benchmark system, along with one possible damping control solution for it.

A. Benchmark 1: Three-machine infinite-bus (3MIB) system

This system is comprised of 6 buses and 3 generators, as shown in Fig. 1, in which generators 1 and 2 are identical parallel units of the same power plant. The 3MIB system exhibits all three types of electromechanical modes, which can be classified into intra-plant (between generating units 1 and 2), inter-plant or local (parallel units 1 and 2 against generator

design methods implementing this solution for this system have been proposed in [9], some utilizing modern robust control techniques, but all based on decentralized control for reasons explained in [9]. In the proposed solution for the benchmark, PSSs are provided at all the generators, except at generator 7 (given that it is an area equivalent). The PSS of each generator is tuned independently (with the PSSs of the generators disabled) with the objective of providing maximum damping to the two inter-area modes. A classical PSS design technique has been used for tuning the PSSs [6].

C. Benchmark 3: 2-areas, 4-generators system

B. Benchmark 2: Brazilian 7-bus equivalent system

Due to its symmetric structure, the two local modes related to areas 1 and 2 can have almost identical frequencies (depending on the power flow conditions, among other factors [3]). The inter-area oscillation between areas 1 and 2 has a lower frequency than the local modes, as expected. The system poses the challenge of simultaneous damping of local and inter-area modes in a system with a symmetrical structure.

Reference [5] presents the original data for the PSS and also a modified PSS tuning leading to a much closer match to the required phase compensation, based on conventional methods [12], [6] for PSS tuning that are still very effective and widely used in field tuning of PSSs [15]. All modes in the benchmark can be properly damped simply by a suitable coordination of PSSs. Given that conventionally tuned PSSs can provide effective damping to this system the justification for a novel POD or PSS tuning method for this system would need to be particularly compelling.

D. Benchmark 4: 39-bus New England test system

Almost all electromechanical modes in this system have local or regional nature, except for one that is observed as the oscillation of generators 2 to 10 against generator 1. This latter mode has the lowest frequency and should be regarded as a New England versus New York inter-area mode, with all generators within the New England area oscillating coherently against the New York equivalent (generator 1).

One possible solution to eliminate the problematic NMP zeroes, and thus allow the Itaipu PSS to push the unstable open-loop pole further to the left in the complex plane, is to install another PSS in at least a second machine. Several PSS

This system does not present much of a challenge from the small-signal stability stabilization viewpoint and is included herein mostly for historical reasons and for the sake of verifying the compatibility of results from different software. The most interesting feature of this system is the challenge of coordinating the actions of multiple PSSs in order to damp multiple modes. The emphasis of the presented results is on avoiding detrimental interactions among the multiple PSSs that have to provide adequate damping for both the local mode of their respective generators and the inter-area mode that involves all generators against the New York equivalent.

Fig. 4 - Single-line diagram of the 39-bus system

The applied solution was based on a classical tuning method, which involved the calculation of the $GEP(s)$ function of each of the system generators and the determination of PSS gains and phase compensation parameters according to the guidelines given in [6].

E. Benchmark 5: Australian 14-generator equivalent system

This simplified model of the southern and eastern Australian system, shown in Fig. 5, consists of 59 buses, 14 generators and 5 areas. The system also includes five Static VAR Compensators (SVCs) and a series compensated transmission line. This system is characterized by four weakly connected regions resulting in three inter-area modes of oscillation as well as 10 local area modes. Base cases are provided for an encompassing set of six different system operating conditions representing a range of system loading and interconnection power flow conditions. A comprehensive set of transient stability analysis results for two-phase to ground faults at all system buses are provided for each of the six study cases via [5].

The challenge posed by this system is simultaneous damping of all the local and inter-area modes using PSSs such that the damping remains robust for multiple operating points. As mentioned, PSS performance following large disturbances is also assessed.

The solution chosen in this case is based on the “P-Vr” PSS-design method [19] which is applied widely in practice. The P-Vr characteristic of a generator is the frequency response from the AVR voltage reference “Vr” to the electric-torque (or equivalently electrical power output “P”) with the shaft dynamics of all machines disabled [19]. The P-Vr characteristic is computed for each generator in each study case. For the i^{th} generator one of the P-Vr characteristics from the six-study cases one is selected as representative for the purpose of PSS tuning. A “best fit” low-order transfer-function

representation, $H_i(s)$, of the selected P-Vr characteristic is found for the i^{th} generator. Tuning of the PSS compensation is based on the concept that the damping-torque coefficients introduced by the PSS fitted to the i^{th} generator are given by $D_i(s) = De_i \cdot B_i(s) \cdot G_i(s)$ in which De_i is the desired damping torque coefficient to be introduced by the PSS over the frequency range of electromechanical modes (typically 0.2 to 2 Hz), $B_i(s)$ is a pass band filter with unity gain and near zero phase in the above frequency range and $G_i(s)$ is the PSS transfer-function. Note that this method not only provides phase compensation but also provides a meaningful basis for specifying the PSS gain in terms of desired torque coefficient De_i . Because of the more-or-less invariant nature of the P-Vr characteristics over a wide range of operating conditions, the corresponding designed PSS is robust [19], [20].

Fig. 5 - Single-line diagram of the 14-generator system

F. Benchmark 6: 68-bus system

The 68-bus 5-area system is a reduced order equivalent of the interconnected New England test system (NETS) and New York power system (NYPS) as shown in Fig. 6. There are four inter-area modes present in the system, and have high participation from the electromechanical states of generators 14, 15 and 16 (which represent areas 3, 4 and 5, respectively).

The challenge in this system resides in its difficulty to damp its local and inter-area modes simultaneously. An interesting research problem for this system is whether it is possible to get adequate damping for the inter-area modes without relying on PODs and by only using PSSs.

The 68-bus system is a widely studied system [21], and several solutions for robust damping of all the electromechanical modes in the system are available [22], [23], [24]. Out of these solutions, only [24] relies solely on PSSs for providing robust damping. A shortcoming of [24] is the assumption that all the generators in the system can be controlled using PSSs, but generators 13 to 16 are area-equivalents and PSSs cannot be practically located on these generators. Also, as the inter-area modes have high participation from generators 13 to 16, it is highly probable that these modes cannot be damped by

PSSs alone and hence wide area measurement systems (WAMS) and wide area control-device(s), such as FACTS devices, are needed to adequately damp them. This is one of the challenges offered by this system, and provides wide scope for research as currently there is no solution for damping control which is solely based on PSSs. As study of WAMS and FACTS is outside the scope of this TF, the study and validation of this system has been performed without considering any PODs, except the PSSs on generators 1 to 12. As a feasible solution for PSS design is not available, GEP based classical methods have been used for PSS design for this system [6].

Fig. 6 - Single-line diagram of the 68-bus system

IV. MODELING AND VALIDATION

The dynamic elements of the benchmark systems are modeled according with the guidelines from IEEE standards. Unless noted elsewhere, all the generators are modeled according to IEEE Std. 1110 [25], while excitation systems and PSSs are modeled as per IEEE Std. 421.5 [26]. Salient pole generators are represented by the fifth order IEEE 2.1 model, while round rotor units are represented by the sixth order IEEE 2.2 model. The systems were implemented on at least two widely used commercial software packages. The results of power-flow, eigenvalue calculation and non-linear time-domain simulations are summarized in [5]. In general, the assessment was performed at a single operating point.

The non-linear simulations involved applying step changes to the AVR set points (V_{ref}) or mechanical power inputs of the generators, and also the connection of a shunt reactor at a judiciously chosen bus. The disturbances were selected to excite particular electromechanical modes and assess the damping effectiveness of the proposed stabilizers.

A benchmark system is deemed to be validated if reasonable agreement is obtained between corresponding results from each of the selected software packages. The details of modeling, implementation and validation for each benchmark system are available in [5], and a brief summary of the validation activities is outlined as follows.

A. Benchmark 1: 3MIB system

Generators 1 and 2 of this system are salient pole units, while generator 3 has a round rotor. Each generator is equipped with a static excitation system and a rotor speed-based PSS, represented by the simplified ST1A and PSS1A models, respectively. The two loads are represented by a combination of constant impedance and constant power static models.

The 3MIB system was implemented on the software PSS/E [27] and PacDyn/ANATEM [28], [29]. For the time-domain validation, the simulated disturbances were: (a) a +2% step applied to V_{ref} of all generators at $t = 1$ s; (b) connection of a 50 MVar reactor to bus 5 at $t = 1$ s during 0.1 s, to excite the inter-area mode. Sample results are pictured in Fig. 7 and Fig. 8, respectively.

Fig. 7 - 3MIB system eigenvalues: a) Complete spectrum without PSSs; b) Enlarged view of the electromechanical modes.

Fig. 8 - 3MIB system: Simulation results for case (a).

Fig. 7 and Fig. 8 show that the two software produced matching results, also validating the benchmark system.

B. Benchmark 2: 7-bus system

In this system, all the generators are salient pole units, and except for generator 7 (which is an area equivalent), have a static excitation system ST1A and a PSS1A stabilizer. The loads have a constant current characteristic for the active part and constant admittance for the reactive part.

This implementation was also made on PSS/E and PacDyn/ANATEM. The simulated perturbations were: (a) a +2% step in V_{ref} of generator 4 (Itaipu) at $t = 1$ s; (b) connection of a 500 MVar reactor to bus 6 at $t = 1$ s during 10 s. Both disturbances excite an inter-area mode of 0.85 Hz, which is unstable without PSSs. Sample results are shown in Fig. 9 and Fig. 10, respectively.

Fig. 9 – 7-bus system eigenvalues: a) Complete set without PSSs; b) Enlarged view in the region of electromechanical modes

Fig. 10 – 7-bus system: Simulation results for case (a).

A good matching between the simulation results of the two software was obtained. Also, the results serve the intended purpose of the benchmark system, which is then considered validated.

C. Benchmark 3: 4-generator system

In this system, all the generators are round rotor units represented by the sixth order IEEE 2.2 model. Each generator is equipped with a slow DC excitation system (DC1A) and PSS (PSS1A). The loads have a constant current characteristic for active power and a constant admittance characteristic for reactive power.

This system has been implemented and validated on PSS/E and PacDyn/ANATEM for six operating conditions (the operating cases are taken from [14]). The comparisons of the electromechanical modes for operating case 5 are shown in Table 2. For PSS/E, two sub-packages have been used to calculate the eigenvalues. Results from PSS/E and PacDyn exhibit a close matching in the imaginary parts of all the eigenvalues. However, regarding the real parts, the sub-package LSYSAN for PSS/E provides reasonably close matching to PacDyn results only for the local modes, while the sub-package PSSPLT provides better matching for the inter-area mode.

With respect to the non-linear time-domain simulations, the disturbances applied in all the operating cases correspond to simultaneous changes in V_{ref} of all the generators at $t = 1$ s. The changes are +3% for G1, -1% for G2, -3% for G3 and +1% for G4, and all V_{ref} set-points return to their original values at $t = 1.1$ s. These perturbations have been selected as they excite each and every electromechanical mode in the system. The results for one of the generators (generator G1) for one of the operating cases (case 6) are shown in Fig. 11. The time-domain simulation results exhibit nearly perfect match for the

two software packages, and it is concluded that the 4-generator benchmark system has been validated.

Table 2- 4-generator system: comparison of eigenvalues

Mode type	PSS/E (LSYSAN)	PSS/E (PSSPLT)	PacDyn
Local mode- Area 1 (G1xG2)	$-0.656 \pm j7.09$	$-0.575 \pm j7.06$	$-0.639 \pm j7.08$
Local mode- Area 2 (G3xG4)	$-0.660 \pm j7.29$	Not Provided	$-0.639 \pm j7.28$
Inter-area mode- ((G1+G2)x(G3+G4))	$0.006 \pm j3.84$	$0.038 \pm j3.82$	$0.022 \pm j3.82$

Fig. 11 – 4-generator system: Some simulation results

D. Benchmark 4: 39-bus system

The Task Force has made a choice to be faithful to the original source of data for this system, as given in [16] and [17]. Hence, in this system all the generators are represented by the fourth order IEEE 2.0 model (each generator is a round rotor type unit). Each generator has a static excitation system (simplified ST1A) and a PSS (simplified PSS1A). All the loads are of constant impedance type.

This system has been implemented on three software: MATLAB [30], PacDyn and EMTP-RV [31]. Out of these, the time domain simulations have been performed only on EMTP-RV, and hence cannot be used for validation (as results from at least two packages are required for validation). These simulation results are available in [5]. Exceptionally, only the results of eigenvalue analysis obtained on MATLAB and PacDyn were used for validation of the system. The nine electromechanical modes of this system are displayed in Fig. 12.

Fig. 12 - 39-bus system: Electromechanical modes (with PSS)

It can be observed that the two packages exhibit very good matching. The 39-bus system is validated as a strong matching

is obtained for the rest of the eigenvalues of the system as well.

E. Benchmark 5: 14-generator system

The generators are represented using the “Classical Parameter Model” as described in Section 4.2.13 of [19]. The salient-pole generators HPS1 and YPS3 are represented with two d-axis and one q-axis rotor winding and all others are round-rotor machines represented with two rotor windings in each axis. Generators EPS2, YPS3 and NPS5 have AC1A excitation systems. The rest of the generators has ST1A excitation systems and is equipped with a PSS1A. All the loads are of constant impedance type.

This system has been implemented and validated on MudPack [32], PSS/E, SSAT/TSAT [33] and PacDyn/ANATEM. As an example, Fig. 13 compares, for Case 2, the electromechanical modes obtained with the PSSs in- and out-of-service obtained with Mudpack, PacDyn and SSAT. This reveals the significant left shift of the electromechanical modes due to the PSSs and the very close agreement between the three eigenanalysis packages. A range of simulations has been conducted in a number of the above software and close agreement between them has, in general, been observed. Where differences are observed it has been confirmed that they are due to specific differences in the modelling of some devices. One such comparison is shown in Fig.14.

Fig. 13 – 14-generator system, case 2: Comparison of electromechanical modes with PSSs in- (ON) and out-of-service (OFF).

Fig. 14 – 14-gen system, case 2: Comparison of generator power outputs with two-phase to ground fault applied to bus 209.

The 14-generator benchmark system is considered validated as very good matching is obtained for the results on the software packages.

F. Benchmark 6: 68-bus system

In this system, all the generators are of round rotor type (represented by the sixth order IEEE 2.2 model). All generators have DC excitation systems (DC4B), except for Generator 9 which has a static excitation system ST1A. Generators 1 to 12 are also equipped with PSSs (simplified PSS1A with three lead-lag stages). All the loads are of constant impedance type.

This system has been implemented and validated on MATLAB and PacDyn. For the two cases simulated, in case (a) a step of 2% in V_{ref} is applied to the AVR of generator 3 at $t = 1$ s, and -2% at $t = 11$ s, while in case (b) a 50 MVar reactor is added to bus 3 at $t = 1$ s, and removed at $t = 11$ s. Both disturbances excite the inter-area modes. Some results are shown for eigenvalue analysis and the nonlinear simulations in Fig. 15 and Fig. 16, respectively. The 68-bus benchmark system has been validated as it shows very high degree of matching in the results for the two software packages.

Fig. 15 – 68-bus system: Plots of eigenvalues

Simulation case (a): Generator 3 results (with PSS on generators 1 to 12)

Fig. 16 – 68-bus system: Some simulation results

V. SUMMARY

Six multi-machine systems were selected from the literature and recommended as benchmarks to allow comparison and validation of new methods for the analysis and control of small-signal dynamics in power systems. These benchmark systems have been described in the associated Task Force report “Benchmark Systems for Small-Signal Stability and Control” and their full dynamic data and ample simulation results made available at resourcecenter.ieee-pes.org/pes/product/technical-reports/PESTR18. Details on the structure, research challenge involved, control methodology,

implementation and validation for each benchmark system can be found in the report. Alternatively, computer files with data and simulation results can be downloaded from the TF website ewh.ieee.org/soc/pes/psdpc/PSDP_benchmark_systems.htm.

This paper provides a summary of the TF guidelines for ensuring adherence to minimum quality standards in future research in small-signal stability analysis and control.

The proposed benchmarks may lead to the creation of other test systems for use in future research on power systems facing high penetration of intermittent generation or damping control alternatives derived from remote PMU signals, for example. An important by-product of this TF was ascertaining that the several power system analysis software utilized produced equivalent dynamic simulation results for the benchmark systems. The consistent matching of results helped increase the confidence on power system dynamic simulations tools for dynamic and control studies.

Eventual fixes in the TF documents and files will be made according with demand and under the responsibility of the WG on Dynamic Security Assessment.

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