Strings-to-Rings Transition and Anti-parallel Dipole Alignment in Two-Dimensional Methanols

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Abstract

Structural order emerging in the liquid state necessitates a critical degree of anisotropy of the molecules. For example, liquid crystals and Langmuir monolayers require rod/disc-shaped and long chain amphiphilic molecules, respectively, to break the isotropic symmetry of liquids. In this paper we present results from molecular dynamics simulations demonstrating that in two-dimensional liquids, a significantly smaller degree of anisotropy is sufficient to allow structural organization. In fact, the condensed phase of the smallest amphiphilic molecule, methanol, confined between two, or adsorbed on, graphene sheets forms a monolayer characterized by long chains of molecules. Intra-chain interactions are dominated by hydrogen bonds, whereas inter-chain interactions are dispersive. Upon a decrease in density toward a gas-like state, these strings are transformed into rings. The two-dimensional liquid phase of methanol undergoes another transition upon cooling; in this case, the order-disorder transition is characterized by a low-temperature phase in which the hydrogen bond dipoles of neighboring strings adopt anti-parallel orientation.

Keywords

Two-Dimensional System, Fluids Under Confinement, Order-Disorder Transition, Self-Organization, Amphiphilic Molecules

Text

It is well known that in two dimensional systems thermal fluctuations can completely suppress long-range translational order\(^1,2\). Furthermore, the balance between the changes in entropy and enthalpy across the transition from the isotropic liquid to the ordered crystalline state is not equal to its three-dimensional counterpart, impeding or promoting the freezing transition. The behavior in reduced dimensionality can be also coupled to the chemical or shape anisotropy of the molecules. Water under different confinements has been subject to many investigations\(^3-8\), however, it is lacking any
significant degree of anisotropy. One of the simplest anisotropic molecules is methanol. As of yet, its liquid state in confined geometries has been studied only inside cylindrical nanotubes$^{9-17}$.

In this work we investigated monolayers of methanols that are either confined between two graphenes or freely adsorbed on a single graphene sheet. Figure 1 displays the fraction of methanol molecules participating in strings (chains) and rings structural elements. In the condensed phase at high densities, the methanols are organized predominantly in chains of molecules in which each methanol inside the chain accepts one hydrogen bond and donates another. As the density is decreased toward the gas phase, these strings are transformed into rings. Figure 2 exhibits three instantaneous configurations of the simulation box along this transition. The 'backbone' of these strings and rings is a sequence of hydrogen bonds between the hydroxyl groups. There are also, albeit weaker, dispersion interactions between adjacent methyl groups. The latter, nonetheless, are responsible for the interactions between the structural elements. At intermediate densities (e.g., $\rho_{2D}={2.88\, \text{nm}^{-2}}$), strings coexist alongside rings, however, no phase separation was observed in any of the systems studied. Figure S1 and Fig. S2a in the Supporting Information indicate that the average length of the strings rises linearly as the 2D density increases, with values in the range of 4–13 molecules long, and exhibits a maximum around $\rho_{2D}={5.76}$ and $4.80\, \text{nm}^{-2}$ for the confined and adsorbed systems, respectively. In comparison, the average chain length of bulk methanol was found to be 2.7 molecules long$^{18}$. In contrast to the behavior of strings, four- and five-member rings are by far the most abundant ring sizes, barely affected by the 2D density (Fig. S2b and Table S1).

Apart from the difference in the shape and size of the two motifs, strings and rings differ also in the way the methanol molecules are arranged with respect to one another along the structural motif. In general, strings are composed of chains of methanols in which the methyl groups of neighboring molecules point in opposite directions, forming a zig-zag pattern. Obviously, at finite temperature this pattern is subject to defects as shown in a snapshot in Fig. S3a taken from a simulation at $T=300\, \text{K}$. With a decrease in temperature, there is a reduction of these defects as
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demonstrated in Fig. S3b. In this case, the only defect from a perfect zig-zag arrangement permits
the chain to adopt a kink. In fact, infinitely long zig-zag chains of molecules have been reported
to occur in the crystal structure of methanol in three dimensions\textsuperscript{19–22}, as well as, in a monolayer
film adsorbed on graphite\textsuperscript{23}. In contrast to strings, rings are arranged by methanols pointing their
methyl groups only outwards (Fig. S3c and Fig. S3d). As is the case for the defect mentioned
above, when the methyl groups reside on the same side, their excluded volumes force a bend in
the linear chain and consequently induces formation of a circular shape.

Why do strings appear at high densities and rings at low densities? The packing efficiency of
strings is higher than that of rings and therefore they are found at higher 2D densities. At lower
densities approaching the gas phase, the entropy of the particles is a dominant factor dictating
its phase state. Thus, the methanol molecules will tend to maximize the number of independent
structural elements. Short strings with only one hydrogen bonds at the edges pose a large enthalpic
penalty relative to their size. A way to circumvent that is to form rings. The most probable sizes
observed of four- and five-member rings are likely to be a consequence of the balance between the
strain of the ring and the tendency to maximize their number.

In a series of simulations in which we varied the temperature at a fixed 2D density in the
condensed phase ($\rho_{2D} = 5.76 \text{ nm}^{-2}$), our algorithm for the calculations of structural elements found
that at lower temperatures the fraction of rings increases on the expense of strings. However, visual
inspections of these rings identified them as actually large strings in which both ends are connected
(see Fig. S3e). We arrived to this conclusion because the methanols in these 'rings' are arranged
in a zig-zag structure and their packing efficiency is large, properties characterizing strings. Even
in the absence of a quantified descriptor, it is clear that at lower temperatures the lengths of the
strings increases. However, a more interesting observation is that upon lowering the temperature
another transition is found.

In forming a chain of hydrogen bonds, the dipole moments of the -OH covalent bonds, or
alternatively the dipole moments of the hydrogen bonds themselves, are all aligned in the same
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Neighboring chains can then adopt any orientation with respect to this chain. This is indeed the case at high temperature. However, at low temperatures we find a phase characterized by chains oriented anti-parallel to their nearest neighbor chains.

To quantify this order-disorder transition we defined an order parameter, $\Phi$, that measures the angle between the -OH covalent bonds of neighboring methanols that belong to different chains. A random distribution of the hydroxyl dipoles corresponds to $\Phi=0$, whereas, perfect parallel and anti-parallel organizations correspond to $\Phi=+1$ and $\Phi=-1$, respectively. The value of $\Phi$ as a function of temperature is shown in Fig. 3. At high temperatures the magnitude of $\Phi$ is small, however, always on the negative side. This suggests a nearly complete absence of correlations between the orientations of -OH dipoles of different chains. With a decrease in temperature, there is a clear transition toward a state characterized by a large negative value of $\Phi$ pointing to the anti-parallel alignments of the -OH covalent bonds of neighboring chains. Fig. 3 also indicates an almost a complete lack of order in bulk methanol at all temperatures.

The anti-parallel alignment of the hydrogen bond direction of neighboring chains is shown in a close-up snapshot at the top panel of Fig. 4. In the lower panel, snapshots at three different temperatures along the transition are shown. Here the dipole moments of the methanol molecules are colored according to their orientations. The driving force for this ordering is the gain in energy from dipole-dipole interactions. We analyzed in Fig. S4a the energy between the methanol molecules as a function of temperature. The shape of the curve largely mirrors the extent of hydrogen bonds between the methanol molecules (Fig. S4b). However, at temperatures lower than 260 K the energy continues to decrease (larger magnitudes with negative values), whereas, the number of hydrogen bonds per molecule hardly exhibits any change from its saturated value of two. This is likely to be, at least in part, a result of the gain in dipole-dipole energy from the anti-parallel ordering.

In this series of simulations we reduced the temperature until 160 K. Experimentally, a monolayer of methanol adsorbed on graphite freezes at 142 K$^{23}$. Analyzes of the simulation results indicate
that the two-dimensional methanols we studied is in the liquid state above \( T=200 \) and \( 220 \) K for the PME and cutoff simulations, respectively. Only at these temperatures does the lateral mean-squared displacement exhibit an onset of the cage-effect (Fig. S5) where the dynamics is significantly retarded. These temperatures marks the end-points of the transitions of the anti-parallel -OH dipole alignment. The magnitudes of the corresponding diffusion constants (Fig. S5c) indicate that the two-dimensional methanols across this transition experience substantial mobility. However, in the vicinity of the low-temperature end, the values of the diffusion constants, which are on the order of \( 10^{-7} \) cm\(^2\)/s, characterizes liquid-crystalline phases\(^{24,25} \) and, therefore, we cannot exclude a transition to such a phase. Note that we did not find any long range translational order in any of the systems studied (see Fig. S7) excluding the possibility of crystallization. Nevertheless, at low-temperatures the monolayer does exhibit a large degree of ordering (Fig. 4). This apparent discrepancy is because patches of ordered molecules are oriented chaotically with respect to one another. Furthermore, the ordering of the anti-parallel strings of methanols does not seem to develop any spontaneous dipole moment in the system at any point along the transition (Fig. S6), thus in general, the strings oriented in one direction are counter-balanced by strings oriented in the opposite directions.

Liquids in the vicinity of flat hard surfaces exhibit stratification that extents few molecular diameters into the bulk\(^{26,27} \). At low temperatures, the transverse density of the first layer can have a minimal overlap with the adjacent layer. Does this first layer share similar properties as those found for the confined and adsorbed monolayer systems? To this end, we simulated methanols confined between two graphene sheets with a gap size of about \( 4 \) nm (containing 9–10 layers) at different temperatures. The results and instantaneous configurations shown in Fig. S8 reveal that the extensive formation of strings reported above does not occur here. Nevertheless, lowering the temperature slightly increases the size of the strings. Furthermore, the values of the order parameter \( \Phi \) are small; \(-0.11\) and \(-0.07\) for \( T=200 \) and \( 300 \) K, respectively. Thus, the interfacial layer of methanol next to a wall is lacking the structural properties of a two-dimensional system.
The distraction of structural order is likely to be a result of hydrogen bondings with the adjacent layer.

In this work, two-dimensional methanol systems have been shown to undergo two unique structural organizations that do not have apparent counterparts in three dimensions. The closest analogy in 3D systems is the ordering found in the various liquid crystalline phases in which a significant anisotropy of the molecules is required\textsuperscript{28}. In contrast, in two-dimensions a very weak anisotropy is sufficient to introduce self-organization in the gas-like phase or ordering in the liquid (-crystalline) state. This peculiar behavior is likely due to the coupling between the system’s reduced dimensionality and the amphiphilic character of methanol. It is yet to be seen what are the consequences of a larger hydrocarbon chain as is the case for all other alcohols. Note that the results presented in this paper are applicable to molecular model of methanol under confinement, and therefore, require experimental verification. We hope this can be achieved either by using high-resolution transmission electron microscopy\textsuperscript{8} or scanning tunneling microscopy imaging\textsuperscript{29,30}. 
Figure 1: Density-induced strings to rings transition. The fraction of methanols participating in strings (black squares) or rings (red circles) structural elements as a function of their 2D-density (see Methods for details). The fraction of particles that do not fit to either of these definitions are also displayed (green diamonds). In these simulations, the temperature, T=300 K, and the area of a graphene sheet, A=148.4 nm$^2$, are held constants. Filled and empty symbols are results from methanols confined between two graphene sheets 0.83 nm apart in which the electrostatic interactions were calculated by the PME and cut-off methods, respectively. Symbols filled with squared pattern are results from cut-off simulations of methanols adsorbed onto a single graphene.
Figure 2: Snapshots from the confined simulations analyzed in Fig. 1 at three different 2D-densities (nm$^{-2}$) spanning the strings-to-rings transition. The methyl groups, oxygens, and hydrogens are depicted in gray, red, and white, respectively. The confining graphene sheets are not shown for clarity.
Figure 3: Temperature-induced anti-parallel alignment of strings. The order parameter, $\Phi$, measuring the anti-parallel orientation of the -OH covalent bonds of non-hydrogen-bonded nearest neighbor methanols as a function of temperature. The three types of 2D methanol systems (three types of black circles) are the same as those described in Fig. 1 for $\rho_{2D} = 5.76 \text{ nm}^{-2}$. Values obtained for bulk methanol (red squares) are shown for comparison (where filled and empty symbols have the same meanings as in the 2D systems). $\Phi$ is defined by $\Phi = \langle \frac{1}{N} \sum_{i=1}^{N} \cos \theta_i \rangle$ where the sum is performed over all $N$ methanol molecules and the angle brackets denote ensemble average. $\theta_i$ is the angle between the -OH covalent bonds of particle $i$ and its non-hydrogen-bonded nearest neighbor. The latter is identified by the shortest distance between the methyl groups excluding the first three hydrogen-bonded neighbors toward each direction of the chain.
Figure 4: Snapshots from the simulations analyzed in Fig. 3. The top panel displays a zoom of a segment of the simulation box (of confined methanols using the cutoff method at $\rho_{2D} = 5.76$ nm$^{-2}$ and $T=160$ K) characterized by the anti-parallel ordering of the hydrogen bonds (or molecular dipoles) relative to neighboring (which do not belong to the same chain) hydrogen bonds (molecules). Methyl groups, oxygens, and hydrogens are depicted in blue, red, and white colors, respectively. The lower panel shows this order-disorder transition by displaying snapshots from three different temperatures. The arrows in the graphs represent the molecular dipole vectors of methanols encoded in a color according to its angle with respect to a fixed coordinate system. The color bar scale is shown on the right.
Methods

Condensed phase of methanols in two-dimensions was realized either by confining the molecules between two parallel (and in-registry) graphene sheets, 0.83 nm apart, or by adsorbing the methanols onto a single graphene sheet in vacuum. Graphene was chosen as the confining surface because the methanol molecules are not likely to commensurate with its structure. The adsorbed methanol system was constructed by placing each of the graphene sheets, together with the associated adsorbed methanols, 10 nm apart such that these two replica of the system effectively did not interact with each other. In both case, periodic boundary conditions were effectively applied only along the lateral direction ($x$- and $y$-axes). Periodicity along the $z$-axis was suppressed by taking a large (larger than 6 nm) vacuum region above and below the two graphene sheets.

These single-layered graphene sheets, with a fixed dimension of 12.03 nm x 12.33 nm and consisting of 5684 atoms each, interacted (via bonded and non-bonded interactions) with their periodic images along the lateral direction in such a way that they created an infinite surface. To prevent their translations in the simulation box, the atoms of the graphene sheets were restrained by harmonic potentials in all directions with a force constant of 1000 kJ/(mol·nm$^2$). The Lennard-Jones (LJ) parameters for the carbon atoms of the graphenes, $\sigma_{CC}=0.3851$ nm and $\epsilon_{CC}=0.4396$ kJ/mol, were taken from parameterization of single-wall carbon nanotubes$^{31}$ with bonds stretching and angles bending as detailed in our previous work$^{32}$. The methanol molecules were described by the united-atom OPLS force-field$^{33}$ using the geometric combination rules for calculating their interaction with the graphene sheets.

The simulations were performed at constant $N$, $V$, $T$ ensemble in two different series. In the first, the number of methanol molecules varied from 36 to 1105 at constant temperature of 300 K. In this case, we presented the state of the system by the two-dimensional number density $\rho_{2D} = N/A$ where $A$ is the lateral area. Because our aim is to investigate the behavior in two-dimensions, we restricted the states of the system to those exhibiting only a monolayer of methanols. This was the case for all densities in the confined methanol systems, however, for the adsorbed methanol
systems with densities larger than $\rho_{2D}=5.76 \text{ nm}^{-2}$ a second layer starts to develop (see Fig. S9), and therefore, these simulations were not processed. This observation is in agreement with an X-ray diffraction study$^{23}$ which concluded that at 132 K the monolayer capacity of methanol on graphite is about 6 molecule per nm$^2$. In the second series of simulations, we varied the temperature in the range of 160 K and 440 K at a constant number of methanols $N = 855 \left(\rho_{2D}=5.76 \text{ nm}^{-2}\right)$. Bulk methanol boils at 338 K$^{34}$, however, for the adsorbed system at $\rho_{2D}=5.76 \text{ nm}^{-2}$ we did not observe evaporation (except of infrequent instantaneous departures of molecules that could also re-adsorbed at the remote system) even up to $T=360$ K. Nevertheless, at this temperature there was also an onset of a bilayer, and thus, we did not apply higher temperatures for the adsorbed system in this series of simulations. In Fig. S10 we plot the auto-correlation functions for the adsorbed state for $\rho_{2D}=5.76 \text{ nm}^{-2}$ at three different temperatures. This density was chosen because it is characterized by the fastest decay of adsorption. The graph indicates that the average life-time for a methanol molecule on graphene is 2610, 42.5, and 3.7 ns for $T=240, 300$, and 360 K, respectively. Thus, for the relevant temperatures, the corresponding residence times are much longer than the relaxation times characterizing the different structural orders.

We used the molecular dynamics package GROMACS version 4.6.5$^{35}$ to perform all of the computer simulations with a time step of 0.002 ps. The desired temperature was maintained by the velocity rescaling thermostat$^{36}$, applied for the whole system, with a coupling time of 0.1 ps. In light of reports of artifacts that might emerge due to the artificial periodicity imposed by Ewald summation$^{37}$, the simulations were conducted using a cut-off method (twin-ranged of 1.0 nm and 1.4 nm updated every 1 and 5 steps, respectively) for the calculation of the electrostatics and LJ forces. Nevertheless, the confined methanol system was also simulated using the Particle-Meshed Ewald (PME) method$^{38}$, adapted for a slab geometry, for comparison. The cut-off distance of the PME real-space part was 1.0 nm and the grid spacing for the reciprocal-space was 0.12 nm with quadratic interpolation. In this case, the LJ potential was evaluated by a single cutoff distance of 1.0 nm. Although, quantitative differences were noticed in the calculation of $\Phi$ and $D_{xy}$, qualitatively,
these two methods yielded the same results. When using the PME method, long-range electrostatic interactions, and even those from periodic boxes, are taken into account. These excess energetic terms are not likely to be the same for both phases across the transition, and consequently the exact transition point depends on whether they are included or not.

In general, all systems were equilibrated for 80 ns and data collected for additional 80 ns. However, for temperatures below $T=260$ K the systems were further equilibrated for additional 160 ns. The lateral and transverse pressures were calculated from the corresponding internal virials of the methanol molecules. Note that the graphene sheet is built as a periodic surface and, therefore, its virial can not be used to calculate the contribution to the force it exerts on the walls of the simulation box.

The simulations of bulk methanol (in the absence of any confining walls) were performed with 1728 molecules, in a cubic-shaped box, with PME and cutoff methods for calculating the electrostatic forces. Here, in addition to a thermostat, the system was also coupled to a barostat at a pressure of 1.0 bar (with a compressibility of $1 \cdot 10^{-4}$ 1/bar and a coupling time of 1.0 ps).

**Analyzes of the Results**

To compute the distributions of strings and rings formed by the methanol molecules, we determined for each molecule the number of contact neighbors and the list of these neighbors. Particles with zero neighbors were labeled as such. We identify first the strings by starting to check particles that have only one contact neighbor. Then, its neighbor is checked. The assignment of the string element continues as long as the next unvisited neighbor have 2 contact neighbors and it ends when it has only one neighbor. After all one-neighbor molecules were visited, we start the assignment of rings. To this end, we choose unvisited molecules that have two neighbors and continue to the next unvisited neighbor until we reached a molecule in which all its neighbors were visited. This algorithm unambiguously assign strings and rings provided the network does not contains particles with more than two neighbors. In all the systems studied, the fraction of particles with more than two neighbors was less than 0.02. When this situation encountered, we continued with the
identification of the structural element toward the neighbor with the shortest contact (as defined by acceptor-donor distance), whereas the remaining branch was considered independently. Two methanol molecules were considered to be in contact if they formed a hydrogen bond with each other. The latter was defined if the donor–acceptor and hydrogen–acceptor distances were simultaneously smaller than 0.35 nm and 0.25 nm, respectively, and the donor–hydrogen–acceptor angle was larger than 135° (corresponding to the first minimum from linearity in the angle distribution).

**Associated Content**

The Supporting Information contains seven figures and one tables described in the manuscript text.

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**Notes**

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