

Market risk of BRIC Eurobonds in the financial crisis period

- [Dimitrios I. Vortelinos](#),
- [Geeta Lakshmi](#),
- Lincoln Business School, University of Lincoln, UK

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Highlights

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Most significant in terms of risk and jumps are the Chinese, among BRIC Eurobonds.

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Most significant range estimator is the Yang Zhang estimator.

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Higher risk and jumps for theoretical and not actual prices

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Higher expiry period relates to more significant risk and jumps.

Abstract

The market risk of returns for BRIC Eurobonds has not been thoroughly analyzed via nonparametric estimation methods. The significance of risk and jumps is examined in a monthly sampling frequency. A detailed comparison upon significance of risk and jumps between BRIC Eurobonds is provided. Comparison concerns risk and jumps during the international financial crisis period: February 2007 up to February 2010. Among the BRIC countries, Chinese Eurobonds are the most significant in terms of both risk and jumps. The most significant estimator is the monthly Yang & Zhang range across the set of BRIC Eurobonds. The shorter the expiry period, the higher is the significance of risk and jumps. This is evident in all BRIC Eurobonds. Risk and jump estimates are higher for theoretical prices rather than for actual prices according to all risk and jump significance measures.

Keywords

- BRIC Eurobonds;
- Risk;
- Jumps;
- Bond pricing;
- Financial crisis

JEL classification

- [G12](#);
 - [G15](#);
 - [G17](#)
-

1. Introduction

In the last decade, the BRIC² countries have been researched extensively in the economics and finance literature. One of the first studies researching the significant role of the BRIC economies in the contemporary international economy's structure is [Julius \(2005\)](#). Recently, [Aloui, Aissa, and Nguyen \(2011\)](#) showed strong evidence of time-varying dependence between each of the BRIC markets and the US markets. Some of more recent studies on BRIC countries are: [Cakir and Kadundi \(2013\)](#) and [Bekiros \(2014\)](#). [Fang and You \(2014\)](#) investigated how explicit structural shocks that characterize the endogenous character of changes in oil prices affect three of the four BRICs' stock-market returns. Part of this BRIC literature is the BRIC Eurobonds³ literature, which has not been extensively investigated. A recent paper studying the BRIC countries' debt markets is by [Steinbock \(2012\)](#). Specifically in this paper, the prospects for BRIC countries from the Eurozone debt crisis are studied. [Peristiani and Santos \(2010\)](#) reported that the extent of the dominance of the US Eurobond market globally has been reduced as the role of BRIC countries in the international Eurobond market increased. In this paper, BRIC Eurobonds are analyzed using both actual market prices and theoretical prices. Actual prices are the ones obtained in the market. Theoretical prices are obtained by a pricing model (as suggested by [McCulloch, 1971](#)) which involves fitting a smooth discount function (which is a cubic spline). Moreover, literature has also not extensively examined the market risk of BRIC Eurobonds. The present paper examines the significance of both market risk and jumps of risk series in the recent financial crisis period⁴.

Market risk is measured by conditional variance (volatility) that is latent; so, market risk is not directly observable. Literature has concentrated on parametric estimators of volatility, like: (i) Generalized AutoRegressive Conditional Heteroskedasticity (GARCH), (ii) Stochastic Volatility (SV), (iii) Exponentially Weighted Moving Average (EWMA) models, among others. The ex post volatility essentially becomes observable, if the effect of the microstructure noise is low. Contemporary realized volatility estimators, as the ones employed here, minimize such

effect. As volatility becomes observable, it can be modeled directly. [Andersen and Bollerslev \(1998\)](#) introduced the first and most naive realized volatility estimator, as the best nonparametric volatility estimator. Recent literature suggests that the realized volatility estimator is useful for: (i) predicting future volatility ([Byun & Kim, 2013](#)); (ii) asset allocation in portfolios ([Bandi, Russell, & Zhu, 2008](#)); (iii) risk management ([Giot & Laurent, 2004](#)); and (iv) VaR computation ([Clements, Galvao, & Kim, 2008](#)). [Sevi \(2015\)](#) investigated the realized volatility usefulness for modeling the convenience yield. Specifically, monthly realized volatilities and jumps explained convenience yield; whereas, jumps were detected as in [Tauchen and Zhou \(2010\)](#).

The present paper employs the estimation strength of many non-parametric volatility estimators; all belonging to the realized volatility literature. Estimators are classified into three groups: realized volatility estimators, range volatility estimators, and realized range-based volatility estimators. The first group of estimators studied is realized volatility estimators. The non-parametric estimator that most effectively uses data for estimation purposes is realized volatility. [Andersen et al., 2001](#) and [Andersen et al., 2003](#) were the first to theoretically and empirically research realized volatility estimation. There are different parameterizations for the realized volatility estimation literature. Most of the finance literature estimates realized volatility in a daily frequency via intraday data series. However, the present paper estimates monthly volatilities via daily data, because of low intraday and daily liquidity. [Jiang and Tian \(2005\)](#) out-of-sample compares the realized volatility to implied volatility in a monthly frequency. A recent influential study in monthly realized volatility estimation (as well as forecasting) is [Busch, Christensen, and Nielsen \(2011\)](#). A more recent and applied study on realized volatility estimators is [Bollerslev, Osterrieder, Sizova, and Tauchen \(2013\)](#). Another nonparametric volatility estimator is range. The first range estimator was suggested in [Parkinson \(1980\)](#). A recent study in range estimators of volatility is [Louzis, Xanthopoulos-Sisinis, and Refenes \(2013\)](#). A third group of nonparametric estimators is realized range-based volatility estimators. One of the very first papers to research this type of estimators is [Martens and van Dijk \(2007\)](#). A recent study in realized range-based estimators is [Bannouh, Martens, and van Dijk \(2013\)](#).

In the present paper, twelve nonparametric volatility estimators estimate risk. These estimators are split into three categories: realized volatility, monthly range, and realized range-based volatility. The first group includes the 5-minute unrestricted realized volatility ($RV_{t,m}$), the realized bipower variation ($BPV_{t,m}$), a moving average-based volatility that uses the first order residuals ($RV_{t,ma\ adj^1}$), and a moving average-based volatility that uses the second order residuals ($RV_{t,ma\ adj^2}$). The monthly ranges group includes the monthly Parkinson range ($MR_{t,Par}$), the monthly Garman & Klass range ($MR_{t,GK}$), the monthly Rogers & Satchell range ($MR_{t,RS}$), and the monthly Yang & Zhang range ($MR_{t,YZ}$). The third group of realized range-based volatility includes the realized Parkinson range-based volatility ($RR_{t,Par}$), the realized Garman & Klass range-based volatility ($RR_{t,GK}$), the realized Rogers & Satchell

range-based volatility (RR^{RS}), and the realized Yang & Zhang range-based volatility (RR^{YZ}).

Risk (volatility) series is not a continuous process; jumps make this process discontinuous. Jumps can be detected in any time interval. Literature detected and studied jumps in volatility from an intraday sampling frequency⁵ up to a monthly frequency⁶. The present paper studies monthly jumps (in monthly volatility series). The employed detection scheme was introduced in [Ait-Sahalia and Jacod \(2009\)](#)⁷.

The present paper estimates volatility in a monthly frequency, because most of market participants in the Eurobonds market do not aim at intraday capital gains. They mostly trade sovereign bonds either in a daily or most probably in a monthly frequency. Most of them are fund managers or treasurers, pension or hedge fund managers or treasurers, rebalancing their portfolios monthly. So, there is no need to employ intraday high-frequency data. Moreover, there is low liquidity of Eurobonds in an intraday frequency. In this paper, we use non-parametric volatility estimators, as literature suggests due to higher robustness. Studies in the literature have recently estimated realized volatility in a monthly frequency. [Afonso, Gomes, and Taamouti \(2014\)](#) used, as an alternative to parametric volatility models, non-parametric measures of volatility: the absolute value and the squared returns as proxies of monthly volatilities. [An, Ang, Bali, and Cakici \(2014\)](#) employed the monthly realized volatility estimates as a factor in the cross-sectional relation between implied volatility shocks. [Zhu and Lian \(2015\)](#) provided in a monthly frequency two analytical closed-form formulae for the price of forward-start variance swap with the realized variance being defined by the actual-return realized variance and the log-return realized variance. Moreover, [Lee, Paek, Ha, and Ko \(2015\)](#) employed a structural VAR model for examining the relations among monthly realized volatility, market return, and aggregate equity fund flows in an international context. [Seo and Kim \(2015\)](#) examined the effect of investor sentiment on the relationship between the option-implied information and the future stock return monthly realized volatility. Moreover, more accurate estimators are employed for nonparametrically estimating monthly realized volatility in this paper.

This study contributes to the literature through the following aspects. To the best of our knowledge, this present study is the first to nonparametrically examine the significance of risk and jumps of BRIC Eurobonds. Secondly, many realized volatility estimators are employed. Risk is estimated via twelve nonparametric estimators as split into three groups (realized volatility, range, and realized range-based volatility). The significance of risk is measured via the mean magnitude of risk (\bar{R}) and the mean Sharpe ratio (\bar{SR}) as well. Thirdly, two jump detection schemes are employed for risk jumps. The significance of jumps is measured via the mean magnitude of jumps (\bar{J}), the mean magnitude of the jump component of risk relative to the magnitude of the continuous component (\bar{J}^R), the average frequency of jump occurrence (\bar{J}), and the average frequency of occurrence of statistically significant jumps (\bar{J}^+). Fourthly, volatility estimates concern both actual and theoretical prices.

The remainder of the article is structured as follows. The second section describes the data and provides a descriptive analysis of returns. The third section presents the methodology. The fourth section discusses on empirical findings. The fifth section summarizes and concludes.

2. Data

2.1. Data description

The sample covers the period from February 2007 to February 2010, a total of 717 trading days or 37 months. Data relates to actual (market) prices of ten Eurobonds from all BRIC countries (Brazil, Russia, India and China). BRIC member countries together encompass over 25% of the world's land coverage, 40% of the world's population, and about 25% of the global GDP in 2010, with significant increases in global GDP share expected over the next four decades.

The sovereign bond ratings from Moody's for the BRIC countries are: Brazil (BBB -), Russia (BBB +), India (BBB -) and China (A +)⁸. There are similarities as well as some differences between the stock exchanges of the BRIC countries. According to [Table 1](#), China is ranked first and Russia last among BRIC countries in terms of market capitalization, market capitalization to GDP, the MSCI Emerging markets index weights and the S&P/IFC EM Index weights. Brazil and India are ranked in between. China is also ranked first in terms of GDP growth, with India second, Russia third and Brazil last.

Table 1.

BRIC countries' stock exchanges.

Country	GDP growth (%)	Exchange	Market capitalization	Market capitalization to GDP (%)	MSCI emerging markets index weights	S&P/IFC EM index weights
Brazil	5.08	BM & FBOVESPA	1,337,248	74.26	16.90%	11.99%
Russia	5.60	MICEX	736,307	69.99	6.30%	6.45%
India	6.07	Bombay SE	1,306,520	90.01	7.50%	7.39%
China	9.00	Shanghai SE	2,704,778	100.46	17.90%	17.29%

Notes. [Table 1](#) reports the name of the major stock exchange of each of the BRIC countries, as well as the market capitalization, market capitalization to GDP, the country-weights in the MSCI Emerging markets index, and the S&P/IFC EM Index weights. Market capitalization is in \$ millions. [Table 1](#) depicts data for the year 2010 coming from the WFSE (World Federation of Stock Exchanges) historical statistics; only the GDP growth (as a %) is provided by the World Bank.

[Table 2](#) provides the symbol, description, country of origin, expiry year as well as an indication for either actual (market) or theoretical prices. Each country's Eurobonds market is analyzed by three Eurobonds with the only exception being India for which only one Eurobond is employed. The expiry year differs across these Eurobonds. Two Eurobonds expired in late 2010, one in 2011, one in 2012, one in 2013, three expired in 2014, one will expire in 2015

and one in 2016. Daily bond prices have been used to estimate Eurobonds' monthly risk and monthly jumps, as the monthly frequency is appropriate not for traders but for long-term investors (mostly, pension funds) in Eurobond markets.

Table 2.

BRIC countries' Eurobonds.

Symbol	Description	Country	Expiry year	The/Act
<i>B14_{act}</i>	brazil_7_14_2014	Brazil	2014	Act.
<i>B14_{the}</i>	brazil_7_14_2014	Brazil	2014	The.
<i>B11_{act}</i>	brazil_8_7_2011	Brazil	2011	Act.
<i>B11_{the}</i>	brazil_8_7_2011	Brazil	2011	The.
<i>B12_{act}</i>	brazil_1_11_2012	Brazil	2012	Act.
<i>B12_{the}</i>	brazil_1_11_2012	Brazil	2012	The.
<i>R13_{act}</i>	russian_agri_5_16_2013	Russia	2013	Act.
<i>R13_{the}</i>	russian_agri_5_16_2013	Russia	2013	The.
<i>R10_{act1}</i>	bank_of_moscow_11_26_2010	Russia	2010	Act.
<i>R10_{the1}</i>	bank_of_moscow_11_26_2010	Russia	2010	The.
<i>R10_{act2}</i>	bank_of_moscow_11_29_2010	Russia	2010	Act.
<i>R10_{the2}</i>	bank_of_moscow_11_29_2010	Russia	2010	The.
<i>I16_{act}</i>	ntpc_india_3_2_2016	India	2016	Act.
<i>I16_{the}</i>	ntpc_india_3_2_2016	India	2016	The.
<i>C14_{act1}</i>	china_dev_bank_10_8_2014	China	2014	Act.
<i>C14_{the1}</i>	china_dev_bank_10_8_2014	China	2014	The.
<i>C14_{act2}</i>	exim_china_7_29_2014	China	2014	Act.
<i>C14_{the2}</i>	exim_china_7_29_2014	China	2014	The.
<i>C15_{act}</i>	china_dev_bank_10_15_2015	China	2015	Act.
<i>C15_{the}</i>	china_dev_bank_10_15_2015	China	2015	The.

Notes. [Table 2](#) reports the symbol, description, country, expiry year, and the indication of actual or theoretical prices series. Theoretical prices are retrieved as in [Section 3.1](#).

2.2. Descriptive analysis

Return is the logarithmic difference between two consecutive prices. [Table 3](#) presents descriptive statistics (mean, standard deviation, skewness and kurtosis) as well as the normality hypothesis results (CVM-test and QQ-test) for returns. The mean return as well as the standard deviation are the highest for the Russian Eurobond, compared to others. Skewness and kurtosis values indicate the distributions of returns in most of the BRIC Eurobonds are skewed to the right (skewness higher than zero) and leptokurtic (kurtosis higher than three). However, the CVM and LB normality tests do not reject the null hypothesis of normality for most of the BRIC Eurobonds.

Table 3.

Returns—descriptive statistics.

	Mean	St. dev.	Skew.	Kurt.	CVM	QQ
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	Mean	St. dev.	Skew.	Kurt.	CVM	QQ
$B14_{act}$	$-2.91e-4$	0.0238	0.1424	6.05	0.1523	21.43
$B14_{the}$	$-3.24e-4$	0.0203	-0.4529	3.33	0.1341	36.13
$B11_{act}$	$-6.26e-4$	0.0131	-0.1145	3.22	0.1052	19.35
$B11_{the}$	$-7.32e-4$	0.0204	-0.852	3.58	0.1141	24.94
$B12_{act}$	-0.0015	0.0184	-0.2023	5.93	0.2604	21.47
$B12_{the}$	-0.0020	0.0183	-1.02	3.18	0.300	44.28 _□
$R13_{act}$	$2.65e-4$	0.0642	-1.90	9.37	0.5757 _□	10.99
$R13_{the}$	$6.94e-4$	0.0171	-0.4896	3.20	0.0813	13.47
$R10_{act_1}$	$-2.94e-4$	0.0576	-1.34	8.72	0.7759 _□	9.65
$R10_{the_1}$	-0.0019	0.0208	-1.04	3.87	0.4109	78.83 _□
$R10_{act_2}$	$1.16e-4$	0.0302	-1.29	7.84	0.5553 _□	16.41
$R10_{the_2}$	$-4.11e-4$	0.0167	-0.7762	4.05	0.2852	13.62
$I16_{act}$	0.0014	0.0262	-0.5784	4.82	0.0688	14.25
$I16_{the}$	0.0018	0.0234	0.9926	5.03	0.0695	12.61
$C14_{act_1}$	0.0018	0.0255	-1.56	9.04	0.2282	22.71
$C14_{the_1}$	0.0023	0.0211	-0.1093	3.71	0.0541	21.56
$C14_{act_2}$	0.0022	0.0461	0.2685	12.19	0.5929 _□	18.03
$C14_{the_2}$	0.0020	0.0189	-0.0681	3.58	0.0933	23.19
$C15_{act}$	0.0029	0.1711	0.0935	15.14	1.56 _□	14.86
$C15_{the}$	0.0022	0.0256	0.1171	4.07	0.0585	29.32

Notes. The mean, standard deviation, skewness and kurtosis values as well as the CVM and QQ test statistics are reported. All descriptive statistics are reported for either actual returns (indicated by *act*) or theoretical returns (indicated by *the*).

□

Indicates significance in 5% significance level.

3. Empirical methodology

Bond prices employed, used both actual market prices and theoretical prices. Returns are produced for both actual and theoretical prices. Monthly point estimates of volatility are estimated through three groups of estimators: realized volatility, range and realized range-based volatility. Then, monthly jumps are detected from two different detection schemes.

3.1. Bond pricing

Using bond prices is more reliable than using yields. This is because yields are retrieved from actual bond prices and may be depended on different maturities and coupons. The pricing model involves fitting a smooth discount function to information obtained from observed prices of straight bonds with various coupons and maturities by estimating the coefficients for a linear combination of smooth approximating functions forming a cubic spline. Any coupon bond price maturing at par value and paying a coupon at time t can be expressed as:

equation(1)

$$P + AI = C \cdot \sum_{i=1}^T \frac{1}{(1 + R_i)^i} + \frac{100}{(1 + R_n)^n}$$

where P = clean price or the price quoted in the market (as % of par value), C = coupon, R_i = discount rate applicable for period i with T as the final maturity date.

Replacing $\frac{1}{(1 + R_i)^i}$ by, returns

equation(2)

$$P + AI = C \cdot \sum_{i=1}^T d_i + 100 \cdot d_n.$$

The discount function d_i can be expressed as a combination of smooth approximating functions and defines the present value of 1 unit of any numeraine receivable in i years. [McCulloch, 1971](#) and [McCulloch, 1975](#) suggested that the discount function d_i can be expressed as:

equation(3)

$$d(i) = 1 + \sum_{j=1}^k a_j f_j(i)$$

where $k f_j(i)$ functions are chosen (the value of k varying with the exact model) to estimate $d(i)$ by a cubic spline and the a_j are the estimated parameters of the linear regression. The $f_j(i)$, ($j = 1, \dots, k$) are chosen so that $f_j(0) = 0$ to force $d(0) = 1$ and to enable it to be smooth and monotonically nonincreasing. Substituting d_i with $d(i)$ in the $P + AI$ equation, the price of a bond maturing in T months and paying a coupon at time i can be expressed as follows:

equation(4)

$$P + AI = C \cdot \sum_{i=1}^T \left[1 + \sum_{j=1}^k a_j f_j(n) \right] + 100 \cdot \left[1 + \sum_{j=1}^k a_j f_j(n) \right].$$

In case of a discrete time, it is employed a discount function with two cubic splines, $k = 5$ and $\sum_{f=1,ka} f(i) = ai + \beta i^2 + \gamma i^3 + \gamma_1 DV_1 i(i - t_1^*)^3 + \gamma_2 DV_2 i(i - t_2^*)^3$. Then the discount factor is

equation(5)

$$D(i) = 1 + ai + \beta i^2 + \gamma i^3 + \gamma_1 DV_1 i(i - t_1^*)^3 + \gamma_2 DV_2 i(i - t_2^*)^3$$

where DV_1 and DV_2 are dummy variables shifting the cubic term of the polynomial for time points. These are the knot points for the cubic spline. When $D(i)$ is substituted in the $P + AI$ equation and an error term is added then, the final form of the pricing model is:

equation(6)

$$P + AI = C \cdot \sum_{i=1}^T \left[T + a \sum h_i + \beta \sum h_i^2 + \gamma \sum h_i^3 + \gamma_1 \sum DV_1 h_i (h_i - t_1^*) + \gamma_2 \sum DV_2 h_i (h_i - t_2^*)^3 \right] + 100 \cdot \left[1 + ah_T + \beta h_T^2 + \gamma h_T^3 + \gamma_1 DV_1 h_T (h_T - t_1^*)^3 + \gamma_2 DV_2 h_T (h_T - t_2^*)^3 \right] + e$$

where P is the clean price, A is the accrued coupon, T is the total number of coupons left, h is the date to the first coupon, $i = 1$ is the number of coupons left to maturity (up to T) and h_i is the date of the last cash flow. DV represents dummy variables representing the spline knots if time left to maturity of the bond is greater than $t_{(i)}^*$. Taking a large cross section of bonds in a market at a point in time with differing market prices, of diverse coupons and times to maturities and using regression allows the estimation of a , β , γ , γ_1 , and γ_2 using the last equation. The error term in the regression ensures that random effects are captured.

Repeating this exercise over time ensures a time series of a , β , γ , γ_1 , and γ_2 .

The estimates of bond prices via the above bond pricing method return the so-called theoretical bond prices, which are indicated as '*the*', and market prices are indicated as '*act*'. The risk and jumps of BRIC Eurobonds are compared across ten Eurobonds and the four countries as well as across twelve volatility estimators which are split in three groups (realized volatility, range, and realized range-based volatility). Each group consists of four estimators.

3.2. Realized volatility estimators

All realized volatility estimators provide monthly point estimates by using daily returns. [Andersen et al. \(2001\)](#) suggested the unrestricted realized volatility estimator ($RV_{t,m}$): equation(7)

$$RV_t^{(m)} = \sum_{i=1}^m r_{i,m}^2$$

where t is the indication of the month, i indicates the trading day in a specific t month and m is the number of trading days per month across all realized volatility and range estimators. This notation is consistent across all volatility estimators. [Barndorff-Nielsen, Hansen, Lunde, and Shephard \(2011\)](#) theoretically and empirically examined the realized bipower variation ($BPV_{t,m}$). In literature, this estimator is employed to detect jumps because the realized bipower variation has no jumps.

equation(8)

$$BPV_t^{(m)} = \mu_p^{-2} \sum_{i=2}^m |r_{i,m}| |r_{i-1,m}|$$

where $\mu_p = E(|Z|^p)$ is the mean of the p th absolute moment of a standard normal distribution. [Hansen, Large, and Lunde \(2008\)](#) constructed a moving average-based volatility estimator that uses the first order MA(1) residuals ($RV_{t,ma\ adj}^{(n)}$):

equation(9)

$$RV_t^{(ma\ adj)} = (1-\theta) \sum_{i=1}^m (\hat{\epsilon}_{i,m})^2$$

where $r_{i,m} = e_{i,m} - \hat{\theta}_1 e_{i-1,m}$, and $\hat{\theta}_1$ is estimated for each the month. The aim is to reduce the autocorrelation in daily returns. This was evident in the QQ-test statistic values in [Table 3](#) as explained in [Section 2.2. Hansen et al. \(2008\)](#) with [Bandi, Russell, and Yang \(2008\)](#) also proposed a moving average-based volatility estimator that uses the q order MA(q) residuals. The q order is selected according to the AIC criterion. This estimator should be more accurate in case of more than one MA orders ($RV_t^{(ma\ adj^2)}$):

equation(10)

$$RV_t^{(ma\ adj^2)} = \frac{(1 - \hat{\theta}_1 - \dots - \hat{\theta}_q)^2}{1 + \hat{\theta}_1^2 + \dots + \hat{\theta}_q^2} RV_t^{(m)}$$

where $r_{i,m} = e_{i,m} - \hat{\theta}_1 e_{i-1,m} - \dots - \hat{\theta}_q e_{i-q,m}$ and $RV_t^{(m)}$ is the unrestricted realized volatility estimator.

3.3. Range-based estimators

Range is the difference between the highest and lowest price. Range estimators are split into two categories: monthly ranges, and realized range-based volatility estimators. The monthly range estimators use the highest and lowest monthly prices per month and symbolized as MR_t . The range estimators, also estimated monthly, using the highest and lowest daily prices per day are entitled as realized range-based volatility estimators and symbolized as RR_t . The present paper examines four monthly ranges as well as their corresponding four realized range-based estimators. These estimators are: Parkinson, Garman & Klass, Rogers & Satchell, and Yang & Zhang; either monthly or realized.

3.3.1. Monthly ranges

[Parkinson \(1980\)](#) defined and empirically analyzed the range estimator. That is why the first version of a range estimator is entitled as Parkinson range. As far as the sampling frequency of the estimator is monthly, it can be called monthly Parkinson estimator:

equation(11)

$$MR_t^{(Par)} = \frac{1}{4 \ln 2} \sum \left[\ln \left(P_{h,t}(m) / P_{l,t}(m) \right) \right]^2$$

where $P_{h,t}(m)$ is the highest monthly price (the highest price of the month) and $P_{l,t}(m)$ is the lowest monthly price (the lowest price of the month). [Garman and Klass \(1980\)](#) extended the Parkinson estimator to:

equation(12)

$$MR_t^{(GK)} = \frac{1}{n} \sum \left\{ \begin{array}{l} 0.511 \cdot \left[\ln \left(P_{h,t}(m) / P_{l,t}(m) \right) \right]^2 - 0.019 \cdot \ln \left(P_{c,t}(m) / P_{o,t}(m) \right) \cdot \ln \left(P_{h,t}(m) \cdot P_{l,t}(m) / P_{o,t}^2(m) \right) \\ - 2 \cdot \ln \left(P_{h,t}(m) / P_{o,t}(m) \right) \cdot \ln \left(P_{l,t}(m) / P_{o,t}(m) \right) - 0.383 \cdot \left[\ln \left(P_{c,t}(m) / P_{o,t}(m) \right) \right]^2 \end{array} \right\}$$

where n is the total number of monthly observations, $P_{c,t}(m)$ is the monthly close price (the closing price per month) and $P_{o,t}(m)$ is the monthly open price (the opening price per

month). [Rogers and Satchell \(1991\)](#) extended the Parkinson estimator, in a similar way to [Garman and Klass \(1980\)](#) estimator, via incorporating monthly open and close prices apart from the monthly high and low prices:

equation(13)

$$MR_t^{(RS)} = \frac{1}{n} \sum \left\{ \ln\left(\frac{P_{h,t}(m)}{P_{c,t}(m)}\right) \cdot \ln\left(\frac{P_{h,t}(m)}{P_{o,t}(m)}\right) + \ln\left(\frac{P_{l,t}(m)}{P_{c,t}(m)}\right) \cdot \ln\left(\frac{P_{l,t}(m)}{P_{o,t}(m)}\right) \right\}$$

[Yang and Zhang \(2000\)](#) incorporated a term for the closed market variance (that is the over-month variance; i.e. a month-effect). So, the monthly Yang and Zhang estimator is defined as: equation(14)

$$MR_t^{(YZ)} = \frac{1}{n-1} \sum \left[\ln\left(\frac{P_{o,t}(m)}{P_{c,t}(m)} - P_{\bar{o},t}(m)\right) \right]^2 + \frac{k}{n-1} \sum \left[\ln\left(\frac{P_{c,t}(m)}{P_{o,t}(m)} - P_{\bar{c},t}(m)\right) \right]^2 + (1-k) \cdot MR_t^{(RS)}$$

where n is the number of months, $P_{\bar{c},t}(m) = \frac{1}{n} \sum \left[\ln\left(\frac{P_{c,t}(T)}{P_{o,t}(T)}\right) \right]$

, $P_{\bar{o},t}(m) = \frac{1}{n} \sum \left[\ln\left(\frac{P_{o,t}(T)}{P_{c,t-1}(T)}\right) \right]$ and $k = \frac{0.34}{1.34 + \frac{n-1}{n}}$. $MR_t^{(RS)}$ is the monthly Rogers &

Satchell range estimator, $P_{c,t}(T)$ is the monthly close price, $P_{o,t}(T)$ is the monthly open price, $P_{h,t}(T)$ is the monthly high price, $P_{l,t}(T)$ is the monthly low price, $P_{\bar{c},t}(T)$ is the average monthly close price (average value of all monthly close prices) and $P_{\bar{o},t}(T)$ is the average monthly open price (average value of all monthly open prices).

3.3.2. Realized range-based

When the four range-based estimators are estimated monthly via daily data, they are known as realized range-based estimators. The realized Parkinson range-based volatility estimator is suggested in [Martens and van Dijk \(2007\)](#) ($RR_t^{(Par)}$) as:

equation(15)

$$RR_t^{(Par)} = \frac{1}{4 \log(2)} \sum_{i=1}^m (h_{i,m} - l_{i,m})^2$$

where m is the number of trading days per month, $h_{i,m} = \ln(P_h(i, m))$, and $l_{i,m} = \ln(P_l(i, m))$ are the within the i th daily interval (per day; daily) high and low logarithmic prices. The realized Garman and Klass range-based estimator ($RR_t^{(GK)}$) is:

equation(16)

$$RR_t^{(GK)} = \frac{1}{n} \sum_{i=1}^m \left[0.511 \cdot R_{i,m,1} - 0.019 \cdot R_{i,m,2} \cdot R_{i,m,3} - 2 \cdot R_{i,m,4} \cdot R_{i,m,5} - 0.383 \cdot R_{i,m,2}^2 \right]$$

where n is the number of

months, $R_{i,m,1} = [\ln(P_h(i, m)/P_l(i, m))]^2$, $R_{i,m,2} = \ln(P_d(i, m)/P_o(i, m))$, $R_{i,m,3} = \ln(P_h(i, m) \cdot P_l(i, m)/P_o^2(i, m))$, $R_{i,m,4} = \ln(P_h(i, m)/P_o(i, m))$, and $R_{i,m,5} = \ln(P_l(i, m)/P_o(i, m))$. [Rogers and Satchell \(1991\)](#)'s

estimator can also be estimated as a realized range-based volatility estimator. So, the realized Rogers and Satchell range-based estimator (RR_t^{RS}) is given by:

equation(17)

$$RR_t^{RS} = \frac{1}{n} \sum_{i=1}^m [\dot{R}_{i,m,1} \cdot \dot{R}_{i,m,2} + \dot{R}_{i,m,3} \cdot \dot{R}_{i,m,4}]$$

where $\dot{R}_{i,m,1} = \ln(P_h(i, m)/P_d(i, m))$, $\dot{R}_{i,m,2} = \ln(P_h(i, m)/P_o(i, m))$, $\dot{R}_{i,m,3} = \ln(P_l(i, m)/P_d(i, m))$, and $\dot{R}_{i,m,4} = \ln(P_l(i, m)/P_o(i, m))$. Finally, the realized Yang and Zhang range-based volatility estimator (RR_t^{YZ}) is given by the following equation:

equation(18)

$$RR_t^{YZ} = \frac{1}{n-1} \sum_{i=1}^m (R_{i,m,1}^*)^2 + \frac{k}{n-1} \sum_{i=1}^m (R_{i,m,2}^*)^2 + (1-k) \cdot RR_t^{RS}$$

where $R_{i,m,1}^* = \ln(P_o(i, m)/P_d(i, m) - P_d(i, m))$, $R_{i,m,2}^* = \ln(P_c(i, m)/P_o(i, m) - P_c(i, m))$

$$, P_o(i, m) = \frac{1}{n} \sum [\ln(P_o(i, m)/P_c(i-1, m))] , P_c(i, m) = \frac{1}{n} \sum [\ln(P_c(i, m)/P_o(i, m))] \text{ and } k = \frac{0.34}{1.34 + \frac{n+1}{n-1}} .$$

3.4. Jumps

The detection scheme employed to detect jumps on the monthly volatility series was introduced in [Ait-Sahalia and Jacod \(2009\)](#) and further examined in [Ait-Sahalia and Jacod \(2011\)](#) and [Ait-Sahalia, Jacod, and Li \(2012\)](#).

All three papers detect a jump in volatility series when there is a significant difference between the realized quarticity of a specific sampling frequency and a multiple of it. The critical value for the test of this jump detection scheme is

equation(19)

$$F_a = 2 - \Phi a \cdot (V) 1/2 I(|Vt| > c_1) Vt + I(|Vt| < c_2) Vt$$

where $c_1 = 0.95$, $c_2 = 0.05$, and V_t is any of either realized volatility estimators or range estimators explained in the previous subsection,

$$V = \frac{160 \cdot (m) \cdot \left(\frac{(m)^3}{\pi^{-1/2} \cdot 16 \cdot \gamma(9/2)} \cdot \sum_{i=1}^m |r_{i,m,1}|^8 |r_{i,m,2}| \right)}{3 \cdot \left(\frac{(m)}{\pi^{-1/2} \cdot 4 \cdot \gamma(5/2)} \cdot \sum_{i=1}^m |r_{i,m,1}|^4 |r_{i,m,2}| \right)^2},$$

$r_{i,m,1} = \ln(P_{c_1}(i, m)/P_{c_1}(i-1, m))$, $r_{i,m,2} = \ln(P_{c_2}(i, m)/P_{c_2}(i-1, m))$, $P_{c_1}(i, m)$ is the daily close prices, and $P_{c_2}(i, m)$ is the daily close prices for the multiple of the first sampling (i.e. daily frequency) ($\ln P_{c_1}(i, m)$). The standardized test statistic is

$$S_{test} = \frac{S-2}{V^{1/2}}$$

$$S = \frac{\sum_{i=1}^m |r_{i,m,1}|^4}{\sum_{i=1}^m |r_{i,m,2}|^4}$$

where $S < F_a$. There are jumps for a month, when $S < F_a$. The empirical results reported below are relied on a significance level of $\alpha = 5\%$.

equation(20)

$$JM_t = \max(|V_t - (V)1/2|, 0)$$

The jump part (JM_t) of any V_t estimator is estimated as in [Andersen, Bollerslev, Frederiksen, and Nielsen \(2010\)](#). Jump frequency (JF_t) is the frequency of occurrence of monthly jump upon the total number of months in sample; so, it is the number of months that jumps are detected, is expressed as a percentage to the total number of months for the examined (either before or after) time period. The indicator of the existence of at least one jump per month can be depicted as: $B_t = \mathbb{1}(JM_t \neq 0)$.

4. Empirical findings

All measures are based on average values of monthly point estimates of risk and jumps. Risk is measured via the mean magnitude of risk (\bar{R}) and the mean Sharpe ratio (\bar{SR}) as well. Results for risk are reported in [Table 6](#) and [Table 7](#) accordingly. The significance of jumps is measured via the mean magnitude of jumps (\bar{J}), the mean ratio of the magnitude of the jump component of risk relative to the magnitude of the continuous component (\bar{JR}), and the average frequency of jump occurrence (\bar{J}). Results for jumps are reported in [Table 8](#), [Table 9](#) and [Table 10](#) respectively.

Table 4.

Risk-descriptive statistics-skewness and kurtosis.

	RV_t <i>m</i>	BPV_t <i>(m)</i>	$RV_{t,ma}$ <i>adj⁽¹⁾</i>	$RV_{t,ma}$ <i>adj⁽²⁾</i>	MR_t <i>Par</i>	MR_{tG} <i>K</i>	MR_{tR} <i>S</i>	MR_{tY} <i>Z</i>	RR_t <i>Par</i>	RR_t <i>GK</i>	RR_{tR} <i>S</i>	RR_t <i>YZ</i>
$B14_{ac}$ <i>t</i>	5.54 (32.4 4)	5.59 (32.8 5)	5.60 (32.86)	5.56 (32.56)	5.38 (31.0 7)	-2.12 (8.41)	-2.11 (7.63)	-2.06 (7.36)	5.57 (32. 7)	5.57 (32. 69)	5.60 (32.9 1)	5.54 (32. 47)
$B14_n$ <i>e</i>	2.75 (9.69)	3.18 (12.0 8)	3.05 (11.34)	4.12 (20.42)	2.49 (8.16)	0.208 7 (1.99)	0.971 0 (3.54)	0.985 3 (3.57)	2.74 (9.5 9)	2.75 (9.6 1)	3.62 (16.3 7)	3.02 (11. 46)
$B11_{ac}$ <i>t</i>	29.4 6 (30.2 1)	5.53 (30.6 2)	6.51 (30.69)	6.43 (30.67)	5.16 (29.4 6)	-1.14 (5.53)	-1.62 (6.51)	-1.60 (6.43)	5.27 (30. 43)	1.06 (5.3 6)	3.30 (20.4 8)	3.40 (20. 56)
$B11_n$ <i>e</i>	1.36 (4.04)	1.86 (6.53)	2.04 (7.58)	2.29 (8.48)	1.11 (2.75)	0.300 8 (2.49)	0.472 (3.02)	0.475 6 (3.03)	2.57 (9.8 8)	1.25 (4.0 0)	0.336 2 (5.75)	1.34 (6.8 6)
$B12_{ac}$ <i>t</i>	5.28 (30.4)	5.37 (31.1)	5.36 (31.11)	5.46 (31.79)	5.25 (30.0)	-1.45 (6.50)	-1.38 (5.09)	-1.35 (4.98)	5.38 (31.	5.37 (31.	5.53 (32.4)	5.30 (30.

	RV_t^m	BPV_t^m	RV_t^{ma} adj ⁽¹⁾	RV_t^{ma} adj ⁽²⁾	MR_t^P	MR_t^G	MR_t^R	MR_t^Y	RR_t^P	RR_t^G	RR_t^R	RR_t^Y
	6)	2)			9)				20)	17)	2)	61)
$B12_e$	5.12 (29.1 2)	5.51 (32.2 3)	5.53 (32.40)	5.67 (33.46)	4.16 (21.4 8)	-0.23 63 (2.12)	-0.50 65 (2.84)	-0.48 64 (2.78)	5.12 (29. 13)	5.12 (29. 09)	5.56 (32.5 8)	5.60 (32. 9)
$R13_t$	2.92 (10.0 6)	2.92 (9.96)	2.93 (10.03)	2.96 (10.15)	4.42 (23.2 2)	-1.72 (4.86)	-1.54 (4.09)	-1.55 (4.15)	2.93 (10. 10)	2.93 (10. 11)	2.85 (9.42)	2.91 (10. 02)
$R13_e$	4.60 (24.8 5)	4.34 (22.3 7)	4.24 (21.46)	3.06 (14.17)	5.24 (30.1 5)	-0.37 9 (3.27)	0.669 9 (5.33)	0.704 3 (5.44)	4.41 (23. 24)	4.43 (23. 37)	4.15 (20.9 5)	4.60 (24. 84)
$R10_{ct_1}$	5.23 (29.7 5)	5.38 (30.9 4)	5.38 (30.96)	5.56 (32.54)	4.21 (21.2 0)	-2.73 (10.1 5)	-2.52 (8.84)	-2.55 (9.00)	5.20 (29. 60)	5.18 (29. 42)	5.27 (30.3 1)	5.23 (29. 78)
$R10_{he_1}$	3.42 (15.2 1)	2.45 (8.00)	2.58 (8.84)	3.13 (13.02)	4.67 (25.6 2)	0.004 2 (2.15)	-0.94 99 (6.57)	-0.90 41 (6.41)	2.25 (8.1 8)	1.43 (4.8 4)	-0.48 06 (2.92)	1.72 (6.5 2)
$R10_{ct_2}$	3.87 (18.1 2)	5.30 (30.4 6)	5.39 (31.20)	4.98 (27.79)	3.29 (13.6 2)	-2.42 (8.47)	-2.07 (6.41)	-2.08 (6.43)	3.74 (17. 09)	3.74 (17. 08)	3.87 (18.1 3)	3.87 (18. 11)
$R10_{he_2}$	2.52 (9.55)	2.76 (9.53)	2.91 (11.36)	3.96 (18.82)	1.69 (4.46)	0.499 5 (2.76)	0.512 2 (2.56)	0.51 (2.56)	2.70 (10. 71)	2.70 (10. 71)	3.03 (13.5 9)	2.52 (9.6 7)
$I16_{act}$	2.63 (9.49)	2.81 (10.4 6)	2.80 (10.27)	2.92 (12.09)	1.75 (5.04)	-0.64 49 (2.80)	-0.65 46 (2.59)	-0.65 (2.59)	2.62 (9.5 3)	2.63 (9.6 1)	2.74 (10.3 7)	2.69 (9.8 0)
$I16_{ne}$	5.53 (32.4 0)	5.55 (32.5 1)	5.50 (32.15)	1.11 (3.33)	5.33 (30.6 9)	-0.36 6 (2.06)	1.90 (9.91)	1.97 (10.2 5)	5.49 (32. 13)	5.50 (32. 16)	5.37 (31.1 9)	5.54 (32. 44)
$C14_{ct_1}$	3.57 (16.0 4)	0.32 79 (2.67)	0.2817 (2.83)	0.2869 (2.83)	3.89 (17.6 4)	4.03 (19.3 8)	4.03 (19.3 8)	3.87 (20.2 1)	3.86 (17. 48)	3.87 (17. 58)	3.81 (17.2 5)	3.90 (17. 70)
$C14_{he_1}$	2.59 (5.72)	3.11 (2.25)	2.97 (2.31)	2.63 (2.32)	1.92 (9.95)	-0.45 75 (12.6 9)	-0.32 32 (11.8 3)	-0.31 9 (10.5 7)	2.71 (10. 56)	2.71 (10. 59)	3.70 (18.3 3)	2.94 (12. 36)
$C14_{ct_2}$	5.42 (32.3 4)	1.83 (30.8)	-0.26 79 (30.76)	-0.26 33 (13.05)	5.53 (31.4 7)	5.34 (9.25)	5.34 (2.68)	3.12 (2.63)	5.49 (32. 01)	5.49 (32. 03)	5.31 (30.5 3)	5.50 (32. 14)
$C14_{he_2}$	3.07 (12.3 4)	3.31 (13.3 5)	3.28 (13.3)	3.43 (15.28)	2.50 (8.65)	-0.40 76 (2.22)	-0.01 95 (2.09)	-0.01 43 (2.10)	3.16 (12. 84)	3.17 (12. 87)	4.20 (21.4 8)	3.44 (15. 12)
$C15_{act}$	4.41 (21.5)	5.21 (29.3)	5.25 (29.78)	5.75 (34.03)	3.85 (15.9)	1.72 (12.9)	4.23 (24.2)	4.32 (24.5)	5.74 (33.)	5.74 (33.)	3.98 (17.8)	5.74 (33.)

	RV_t^m	BPV_t^m	$RV_{t,ma}^{adj^{(1)}}$	$RV_{t,ma}^{adj^{(2)}}$	MR_t^{Par}	$MR_{t,G}^K$	$MR_{t,R}^S$	$MR_{t,Y}^Z$	RR_t^{Par}	RR_t^{GK}	$RR_{t,R}^S$	RR_t^{YZ}
	9)	7)			8)		4)	4)	99)	99)	6)	98)
$C15_{ct}$	5.75 (34.0 3)	5.75 (34.0 3)	5.75 (34.03)	5.75 (34.03)	5.74 (34.0 0)	-2.72 (13.3 1)	4.99 (28.5 8)	5.08 (29.2 1)	5.75 (34. 03)	5.75 (34. 03)	2.52 (8.20)	5.75 (34. 03)

Notes. [Table 4](#) reports the descriptive statistics of skewness (outside brackets) and kurtosis (within brackets) for the risk estimates of both actual and theoretical BRIC Eurobond prices. Risk estimates are split into three groups: realized volatility, monthly range-based, and realized range estimates.

Table 5.

Risk-descriptive statistics—CVM and QQ tests.

	$RV_{t,m}$	BPV_t^m	$RV_{t,ma}^{adj^{(1)}}$	$RV_{t,ma}^{adj^{(2)}}$	$MR_{t,P}^{ar}$	MR_t^{GK}	MR_t^{RS}	$MR_{t,Y}^Z$	$RR_{t,P}^{ar}$	$RR_{t,G}^K$	RR_t^{RS}	$RR_{t,Y}^Z$
$B14_{ct}$	2.02□ (3.29)	2.14□ (2.44)	2.14□ (2.43)	2.17□ (2.77)	2.12□ (3.79)	0.35 87 (52.6 2□)	0.49 24□ (44.5 8□)	0.482 9□ (45.2 6□)	2.07□ (2.94)	2.07□ (2.95)	2.16 □ (2.6 5)	2.03□ (3.24)
$B14_{ct}$	1.20□ (18.2 3)	1.47□ (18.5 4)	1.41□ (18.29)	1.37□ (7.97)	1.13□ (28.9 2)	0.06 34 (28.7 9)	0.12 10 (16.6 8)	0.124 3 (16.7 7)	1.21□ (18.2 4)	1.21□ (18.2 6)	1.37 □ (13. 95)	1.28□ (17.4 2)
$B11_{ct}$	1.48□ (5.33)	1.59□ (4.81)	1.60□ (4.71)	1.72□ (4.65)	1.53□ (6.08)	0.09 83 (47.6 9□)	0.17 57 (39.3 6□)	0.173 0 (39.5 2□)	1.47□ (5.05)	0.382 3 (27.2 8)	1.40 □ (12. 78)	1.21□ (13.0 9)
$B11_{ct}$	0.539 8□ (27.1 2)	0.546 0□ (18.9 4)	0.5384 □(16.7)	0.6118 □ (19.63)	0.557 4□ (54.7 4□)	0.04 17 (24.9 5)	0.03 90 (51.5 2□)	0.039 0 (51.3 5□)	1.18□ (19.0 6)	0.485 6□ (15.7 3)	0.80 90□ (30. 14)	0.841 5□ (31.1 5)
$B12_{ct}$	1.63□ (6.04)	1.70□ (4.51)	1.69□ (4.53)	2.04□ (4.18)	1.82□ (5.63)	0.13 07 (40.0 1□)	0.19 41 (53.2 8□)	0.191 2 (53.6 6□)	1.72□ (5.10)	1.72□ (5.14)	1.94 □ (3.4 6)	1.65□ (5.91)
$B12_{ct}$	1.67□ (4.55)	2.02□ (2.18)	2.04□ (2.10)	2.31□ (1.20)	1.28□ (8.59)	0.06 58 (93.3 6□)	0.03 92 (27.2 5)	0.039 0 (27.6 8)	1.65□ (4.57)	1.65□ (4.61)	2.09 □ (2.0 1)	2.19□ (1.70)
$R13_{ct}$	1.76□ (36.0 7)	1.92□ (32.6)	1.92□ (32.29)	1.84□ (33.77)	1.72□ (18.1 5)	0.82 13□ (124. 67□)	0.76 48□ (129. 35□)	0.761 9□ (128. 22□)	1.79□ (35.8 6)	1.79□ (35.8 5)	1.79 □ (35. 60)	1.76□ (36.1 6)
$R13_{ct}$	1.31□ (8.92)	1.38□ (11.2 7)	1.38□ (11.77)	0.5907 □ (15.56)	1.46□ (4.25)	0.04 35 (34.1 0)	0.09 39 (15.9 5)	0.096 3 (15.7 9)	1.26□ (10.3 1)	1.27□ (10.1 5)	1.21 □ (12. 38)	1.31□ (8.84)
$R10_{ct}$	1.99□ (6.98)	1.10□ (4.25)	1.00□ (4.25)	0.9950 □(3.67)	2.14□ (17.4)	2.36 □	2.37 □	2.31□ (54.7)	2.11□ (7.46)	1.97□ (7.08)	1.85 □	2.09□ (7.04)

	$RV_{t,m}$	$BPV_{t,m}$	$RV_{t,m}^{adj^{(1)}}$	$RV_{t,m}^{adj^{(2)}}$	$MR_{t,P}^{an}$	$MR_{t,GK}$	$MR_{t,RS}$	$MR_{t,Z}$	$RR_{t,P}^{an}$	$RR_{t,GK}$	$RR_{t,RS}$	$RR_{t,Z}$
))			1)	(54.0 7)	(55.8 3)	1)			(5.2 7)	
$R10_{he_1}$	1.25 (14.1 8)	1.28 (22.7 4)	1.26 (21.40)	1.31 (16.33)	1.40 (5.33)	0.04 17 (131. 96)	0.06 61 (88.8 8)	0.063 6 (89.6 6)	0.785 5 (20.9 3)	0.380 1 (23.5 6)	0.30 74 (30. 09)	0.667 4 (24.7 7)
$R10_{ct_2}$	1.99 (17.5 9)	2.08 (4.64)	2.15 (3.80)	2.13 (6.52)	1.98 (26.2 2)	0.80 76 (74.9 7)	0.75 47 (84.3 2)	0.750 8 (84.1 4)	1.98 (19.5 9)	1.98 (19.6 0)	1.99 17. 55)	1.99 (17.6 0)
$R10_{he_2}$	0.878 4 (10.9 5)	1.29 (13.4 4)	1.13 (13.80)	1.46 (12.82)	0.937 9 (15.0 9)	0.05 32 (34.1 8)	0.06 85 (52.4 8)	0.068 7 (52.3 0)	0.886 7 (11.9 0)	0.886 4 (11.9 6)	0.80 51 (11. 28)	0.832 6 (11.1 7)
$M16_{act}$	0.843 5 (20.1 3)	1.01 (14.4 0)	1.04 (14.60)	0.7566 17.01)	0.624 3 (27.9 0)	0.18 06 (169. 59)	0.19 97 (134. 23)	0.198 6 (134. 28)	0.818 9 (20.4 2)	0.822 9 (20.3 0)	0.93 82 (18. 45)	0.885 7 (19.6 7)
$M16_{pe}$	1.87 (1.61)	1.94 (1.68)	1.85 (2.04)	0.3783 (48.79)	1.84 (2.30)	0.06 47 (34.1 0)	0.13 65 (14.0 6)	0.142 9 (13.8 1)	1.80 (1.79)	1.81 (1.77)	1.66 2.6 0)	1.89 (1.55)
$C14_{ct_1}$	1.49 (11.7 4)	1.26 (8.96)	1.25 (8.88)	0.5929 (15.15)	1.26 (14.7 8)	0.05 73 (64.5 8)	0.02 51 (63.1 7)	0.025 8 (63.7 3)	1.42 (12.1 7)	1.43 (12.0 9)	1.31 11. 42)	1.48 (11.6 3)
$C14_{he_1}$	0.669 0 (17.9 2)	0.94 4 (12.1 4)	0.9114 (12.65)	0.7668 (17.31)	0.697 0 (28.3 9)	0.07 54 (53.1 6)	0.12 73 (38.2 2)	0.126 2 (38.2 2)	1.00 (12.1 5)	1.00 (12.0 6)	1.25 7.1 7)	1.05 (10.6 9)
$C14_{ct_2}$	2.03 (1.82)	0.111 9 (3.21)	0.0352 (3.24)	0.0382 (18.13)	2.11 (2.43)	2.03 41.1 0)	2.02 45.9 9)	0.992 1 (47.2 3)	2.07 (2.07)	2.07 (2.05)	2.01 3.5 0)	2.09 (2.00)
$C14_{he_2}$	0.950 7 (12.5 6)	1.20 (10.3 2)	1.16 (10.22)	1.06 (11.22)	0.833 8 (28.3 0)	0.10 27 (52.5 9)	0.03 78 (29.9 4)	0.037 1 (29.9 3)	0.709 1 (17.0 2)	0.712 6 (16.8 8)	0.88 82 (9.1 2)	0.741 14.3 5)
$C15_{ct}$	2.58 (10.3 9)	2.58 (10.3 7)	2.58 (7.01)	2.82 (7.53)	2.41 (7.24)	0.59 93 (2.94)	0.97 53 (2.71)	0.978 8 (0.47 44)	2.76 (0.46 48)	2.76 (0.46 48)	1.96 17. 28)	2.76 (0.46 77)
$C15_{pe}$	2.81 (0.68 57)	2.82 (0.68 80)	2.82 (0.687 5)	2.81 (0.686 8)	2.74 (0.68 26)	0.24 16 (16.5)	1.12 5 (5.04)	1.20 (4.58)	2.85 (0.68 29)	2.85 (0.68 29)	1.59 20. 2)	2.85 (0.68)

	$RV_{t,m}$	BPV_t m	$RV_{t,ma}$ $adj^{(1)}$	$RV_{t,ma}$ $adj^{(2)}$	$MR_{t,P}$ an	MR_t GK	MR_t RS	$MR_{t,Y}$ Z	$RR_{t,P}$ an	$RR_{t,G}$ K	RR_t RS	$RR_{t,Y}$ Z
						0))				21)	

Notes. [Table 5](#) reports the descriptive statistics of CVM (outside brackets) and QQ (within brackets) normality tests for the risk (volatility) estimates of both actual and theoretical BRIC Eurobond prices. Risk (volatility) estimates are split into three groups: realized volatility, monthly range, and realized range estimates.

□

Indicates significance in a 5% significance level.

Table 6.

Average magnitude of risk (\bar{R}).

	$RV_{t,m}$	BPV_t m	$RV_{t,ma}$ $adj^{(1)}$	$RV_{t,ma}$ $adj^{(2)}$	$MR_{t,P}$ an	$MR_{t,G}$ K	$MR_{t,R}$ S	$MR_{t,Y}$ Z	$RR_{t,P}$ an	$RR_{t,G}$ K	$RR_{t,R}$ S	$RR_{t,Y}$ Z
$B14_a$	8.54e	9.32e	9.31e	6.12e	6.50e	5.39e	3.90e	3.60e	5.47e	5.58e	4.94e	8.15e
ct	-4	-4	-4	-4	-4	-5	-5	-5	-4	-4	-4	-4
$B14_t$	0.001	0.002	0.001	7.40e	5.49e	5.54e	4.02e	3.71e	8.18e	8.42e	7.36e	0.001
he	3	0	9	-4	-4	-5	-5	-5	-4	-4	-4	3
$B11_a$	3.06e	3.88e	3.85e	2.16e	1.60e	5.20e	3.77e	3.47e	2.06e	3.30e	1.27e	2.39e
ct	-4	-4	-4	-4	-4	-5	-5	-5	-4	-4	-4	-4
$B11_t$	7.04e	9.10e	9.17e	4.42e	3.29e	5.44e	3.95e	3.64e	3.17e	3.50e	1.22e	3.34e
he	-4	-4	-4	-4	-4	-5	-5	-4	-4	-4	-4	-4
$B12_a$	4.20e	4.34e	4.34e	3.24e	2.76e	5.29e	3.83e	3.53e	3.21e	3.26e	2.91e	4.80e
ct	-4	-4	-4	-4	-4	-5	-5	-4	-4	-4	-4	-4
$B12_t$	0.001	0.002	0.002	7.91e	3.85e	5.36e	3.88e	3.58e	8.88e	9.13e	0.001	0.002
he	3	0	0	-4	-4	-5	-5	-5	-4	-4	0	2
$R13$	0.001	0.001	0.001	0.001	0.002	4.79e	3.49e	3.22e	0.001	0.001	8.62e	0.001
act	5	5	6	3	1	-5	-5	-5	1	2	-4	6
$R13_t$	8.99e	0.001	0.001	4.69e	3.65e	5.18e	3.77e	3.47e	6.27e	6.38e	5.29e	9.75e
he	-4	2	2	-4	-4	-5	-5	-5	-4	-4	-4	-4
$R10$	0.001	0.002	0.002	0.001	0.001	4.87e	3.54e	3.26e	0.001	0.002	0.001	0.003
act_1	8	5	5	3	5	-5	-5	-5	2	5	9	8
$R10_t$	0.001	0.002	0.002	7.25e	4.59e	5.04e	3.65e	3.37e	3.01e	0.003	0.002	0.005
he_1	4	3	2	-4	-4	-5	-5	-5	-4	5	9	2
$R10$	0.001	0.001	0.001	9.49e	0.001	4.97e	3.61e	3.33e	6.94e	7.17e	5.15e	0.001
act_2	4	9	9	-4	1	-5	-5	-5	-4	-4	-4	1
$R10_t$	4.46e	8.66e	7.35e	2.88e	1.35e	5.03e	3.65e	3.36e	3.41e	3.51e	2.85e	5.06e
he_2	-4	-4	-4	-4	-4	-5	-5	-5	-4	-4	-4	-4
$I16_{act}$	8.02e	0.001	0.001	5.78e	3.80e	4.78e	3.46e	3.19e	4.51e	4.68e	4.45e	7.89e
	-4	1	1	-4	-4	-5	-5	-5	-4	-4	-4	-4
$I16_e$	0.002	0.003	0.003	9.00e	8.05e	5.09e	3.69e	3.40e	0.001	0.001	0.001	0.002
	0	1	0	-4	-4	-5	-5	-5	2	3	1	0
$C14$	8.50e	9.24e	9.24e	4.67e	4.07e	4.91e	3.55e	3.28e	6.34e	6.42e	5.09e	9.67e
act_1	-4	-4	-4	-4	-4	-5	-5	-5	-4	-4	-4	-4
$C14_t$	8.29e	0.001	0.001	7.24e	3.90e	4.96e	3.60e	3.32e	5.23e	5.29e	4.79e	8.31e
he_1	-4	2	2	-4	-4	-5	-5	-5	-4	-4	-4	-4

	$RV_{t,m}$	BPV_t <i>m</i>	$RV_{t,ma}$ <i>adj</i> ⁽¹⁾	$RV_{t,ma}$ <i>adj</i> ⁽²⁾	$MR_{t,P}$ <i>an</i>	$MR_{t,G}$ <i>K</i>	$MR_{t,R}$ <i>S</i>	$MR_{t,Y}$ <i>Z</i>	$RR_{t,P}$ <i>an</i>	$RR_{t,G}$ <i>K</i>	$RR_{t,R}$ <i>S</i>	$RR_{t,Y}$ <i>Z</i>
<i>C14</i>	9.81e	0.001	0.001	6.94e	5.85e	4.89e	3.54e	3.27e	9.51e	9.74e	7.93e	0.001
<i>act</i> ₂	-4	1	2	-4	-4	-5	-5	-5	-4	-4	-4	5
<i>C14</i>	7.50e	0.001	0.001	6.23e	3.51e	5.02e	3.64e	3.35e	6.41e	6.50e	5.71e	9.76e
<i>act</i> ₂	-4	2	1	-4	-4	-5	-5	-5	-4	-4	-4	-4
<i>C15</i>	0.001	0.001	0.001	4.21e	6.62e	4.96e	3.58e	3.30e	0.019	0.019	6.52e	0.027
<i>act</i>	4	8	8	-4	-4	-5	-5	-5	2	8	-4	7
<i>C15</i> _{he}	0.025	0.046	0.051	0.020	0.005	4.96e	3.64e	3.36e	0.018	0.019	4.64e	0.026
<i>he</i>	8	8	1	8	1	-5	-5	-5	5	1	-4	8

Notes. [Table 6](#) reports the average magnitude of risk (mean volatility) (\bar{R}) for both actual and theoretical BRIC Eurobond prices. Risk (volatility) estimates are split into three groups: realized volatility, monthly range, and realized range estimates. All average values reported, are t-test significant in a 5% significance level.

Table 7.

Average Sharpe ratio (\bar{SR}).

	$RV_{t,m}$	BPV_t <i>m</i>	$RV_{t,ma}$ <i>adj</i> ⁽¹⁾	$RV_{t,ma}$ <i>adj</i> ⁽²⁾	$MR_{t,P}$ <i>an</i>	$MR_{t,G}$ <i>GK</i>	$MR_{t,R}$ <i>RS</i>	$MR_{t,Y}$ <i>YZ</i>	$RR_{t,P}$ <i>an</i>	$RR_{t,G}$ <i>K</i>	$RR_{t,R}$ <i>S</i>	$RR_{t,Y}$ <i>Z</i>
<i>B14_a</i>	-0.3	-0.3	-0.31	-0.47	-0.4	-5.3	-7.4	-8.0	-0.5	-0.5	-0.5	-0.3
<i>ct</i>	401	117	19	47	467	9	4	8	314	206	879	566
<i>B14_b</i>	-0.2	-0.1	-0.16	-0.43	-0.5	-5.8	-8.0	-8.7	-0.3	-0.3	-0.4	-0.2
<i>e</i>	557	600	79	78	902	5	5	4	962	850	405	446
<i>B11_a</i>	-2.0	-1.6	-1.62	-2.89	-3.9	-12.	-16.	-18.	-3.0	1.90	-4.9	-2.6
<i>ct</i>	4	1			1	02	59	00	4		3	2
<i>B11_b</i>	-1.0	-0.8	-0.79	-1.66	-2.2	-13.	-18.	-20.	-2.3	2.09	-6.0	-2.1
<i>e</i>	4	045	85		3	46	54	11	1		1	9
<i>B12_a</i>	-3.4	-3.3	-3.35	-4.49	-5.2	-27.	-38.	-41.	-4.5	-4.4	-5.0	-3.0
<i>ct</i>	7	5			8	52	00	23	3	7	0	4
<i>B12_b</i>	-1.5	-1.0	-0.96	-2.49	-5.1	-36.	-50.	-54.	-2.2	-2.1	-1.9	-0.9
<i>e</i>	2	1	25		1	68	59	88	1	5	6	048
<i>R13_a</i>	0.170	0.172	0.1695	0.2060	0.130	5.52	7.59	8.24	0.232	0.227	0.307	0.161
<i>ct</i>	9	2			0				7	6	1	2
<i>R13_t</i>	0.771	0.571	0.5736	1.48	1.90	13.3	18.4	20.0	1.11	1.09	1.31	0.712
<i>he</i>	8	3				9	3	0				2
<i>R10</i>	-0.1	-0.1	-0.11	-0.22	-0.1	-6.0	-8.3	-9.0	-0.2	0.116	0.151	0.078
<i>act</i> ₁	595	197	82	35	977	4	2	2	527	0	6	3
<i>R10_t</i>	-1.3	-0.8	-0.84	-2.58	-4.0	-37.	-51.	-55.	-6.2	0.539	0.652	0.360
<i>he</i> ₁	3	068	56		6	04	09	43	0	4	9	5
<i>R10</i>	0.081	0.061	0.0619	0.1218	0.104	2.32	3.20	3.47	0.166	0.161	0.224	0.110
<i>act</i> ₂	1	4			7				3	1	2	6
<i>R10_t</i>	-0.9	-0.4	-0.55	-1.42	-3.0	-8.1	-11.	-12.	-1.2	-1.1	-1.4	-0.8
<i>he</i> ₂	205	741	87		5	7	26	22	1	7	4	123
<i>M6_{act}</i>	1.74	1.24	1.24	2.41	3.67	29.1	40.2	43.7	3.09	2.98	3.13	1.77
						7	9	1				
<i>M6_{he}</i>	0.927	0.586	0.6108	2.02	2.25	35.6	49.1	53.3	1.49	1.43	1.67	0.906
	7	1				6	6	3				3

	$RV_{t,m}$	BPV_t <i>m</i>	$RV_{t,ma}$ <i>adj</i> ⁽¹⁾	$RV_{t,ma}$ <i>adj</i> ⁽²⁾	$MR_{t,P}$ <i>an</i>	MR_t <i>GK</i>	MR_t <i>RS</i>	MR_t <i>YZ</i>	$RR_{t,P}$ <i>an</i>	$RR_{t,G}$ <i>K</i>	$RR_{t,R}$ <i>S</i>	$RR_{t,Y}$ <i>Z</i>
$C14_{act_1}$	2.10	1.93	1.93	3.82	4.38	36.3 4	50.1 8	54.4 4	2.81	2.78	3.50	1.85
$C14_{he_1}$	2.79	1.90	1.89	3.19	5.93	46.5 9	64.2 7	69.7 3	4.42	4.37	4.82	2.78
$C14_{act_2}$	2.20	1.94	1.79	3.12	3.70	44.2 3	61.0 5	66.2 3	2.28	2.22	2.73	1.44
$C14_{act_2}$	2.72	1.70	1.77	3.28	5.82	40.7 3	56.1 6	60.9 3	3.19	3.15	3.58	2.09
$C15_{ct}$	2.04	1.62	1.63	6.90	4.39	58.6 8	81.1 8	88.0 7	0.151 7	0.147 2	4.46	0.105 1
$C15_{he}$	0.084 8	0.046 8	0.0429	0.1052	0.433 7	44.1 8	60.2 2	65.2 9	0.118 6	0.114 8	47.19	0.081 7

Notes. [Table 7](#) reports the average Sharpe ratio (\overline{SR}) for both actual and theoretical BRIC Eurobond prices. Sharpe ratio estimates (SR) are split into the three groups of risk estimators: realized volatility, monthly range, and realized range estimates. All average values reported, are t-test significant in a 5% significance level.

Table 8.

Mean magnitude of jumps (\overline{JM}).

	$RV_{t,m}$	BPV_t <i>m</i>	$RV_{t,ma}$ <i>adj</i> ⁽¹⁾	$RV_{t,ma}$ <i>adj</i> ⁽²⁾	$MR_{t,P}$ <i>an</i>	$MR_{t,G}$ <i>K</i>	$MR_{t,R}$ <i>S</i>	$MR_{t,Y}$ <i>Z</i>	$RR_{t,P}$ <i>an</i>	$RR_{t,G}$ <i>K</i>	$RR_{t,R}$ <i>S</i>	$RR_{t,Y}$ <i>Z</i>
$B14_{ct}$	5.53e -4	6.09e -4	7.60e -4	7.60e -4	1.59e -4	3.21e -5	2.18e -5	2.05e -5	1.26e -4	1.24e -4	5.62e -5	5.78e -4
$B14_{he}$	0.001 3	6.67e -4	0.002 3	0.002 2	5.32e -4	1.71e -5	1.83e -5	1.70e -5	0.001 7	0.002 1	0.001 8	0.002 0
$B11_{ct}$	1.48e -4	1.80e -4	2.21e -4	2.18e -4	4.41e -5	3.31e -5	2.41e -5	2.11e -5	6.51e -5	6.87e -4	3.02e -4	2.59e -4
$B11_{he}$	0.001 3	1.23e -4	5.90e -4	5.97e -4	3.68e -4	3.40e -5	1.95e -5	2.08e -5	6.23e -4	6.23e -4	6.23e -4	6.23e -4
$B12_{ct}$	2.07e -4	2.86e -4	1.93e -4	1.88e -4	6.62e -4	2.60e -5	1.83e -5	1.99e -5	7.60e -5	8.72e -5	7.27e -5	1.33e -4
$B12_{he}$	0.001 6	8.56e -4	0.002 1	0.002 3	3.56e -4	3.30e -5	2.25e -5	2.21e -5	6.14e -4	6.14e -4	6.14e -4	6.14e -4
$R13_{act}$	3.81e -4	0.001 3	7.87e -4	7.84e -4	0.001 5	2.13e -5	1.42e -5	1.14e -5	2.07e -4	2.88e -4	1.26e -4	3.74e -4
$R13_{he}$	0.001 6	4.03e -4	0.001 2	0.001 1	8.35e -4	9.54e -6	9.60e -6	9.18e -6	0.001 9	0.002 0	0.001 5	7.89e -4
$R10_{act_1}$	3.71e -4	0.001 3	0.002 1	0.002 1	7.86e -4	3.20e -5	2.21e -5	2.09e -5	0.002 8	0.003 6	0.002 9	0.005 2
$R10_{he_1}$	6.42e -4	2.72e -4	7.74e -4	6.48e -4	1.88e -4	2.51e -5	1.57e -5	1.45e -5	3.03e -4	0.003 2	0.002 8	0.004 9
$R10_{act_2}$	6.10e -4	6.52e -4	7.95e -4	9.66e -4	3.92e -4	3.02e -5	1.83e -5	1.55e -5	1.69e -4	1.73e -4	6.50e -5	3.46e -4
$R10_{he_2}$	5.57e -4	2.42e -4	8.41e -4	6.27e -4	1.81e -4	2.59e -5	1.44e -5	1.34e -5	2.20e -4	2.31e -4	1.99e -4	2.98e -4

	$RV_{t,m}$	BPV_t m	$RV_{t,ma}$ $adj^{(1)}$	$RV_{t,ma}$ $adj^{(2)}$	$MR_{t,P}$ ar	$MR_{t,G}$ K	$MR_{t,R}$ S	$MR_{t,Y}$ Z	$RR_{t,P}$ ar	$RR_{t,G}$ K	$RR_{t,R}$ S	$RR_{t,Y}$ Z
$I16_{act}$	6.60e -4	5.09e -4	9.27e -4	9.27e -4	1.70e -4	3.52e -5	3.28e -5	3.01e -5	9.98e -4	1.44e -4	6.64e -5	5.61e -4
$I16_{the}$	0.005 3	8.07e -4	0.004 2	0.004 0	0.001 1	4.86e -5	3.42e -5	3.13e -5	0.005 7	0.006 0	0.005 9	0.006 4
$C14_{act,t_1}$	9.85e -4	3.97e -4	6.40e -4	6.39e -4	3.25e -4	2.27e -5	2.36e -5	2.08e -5	5.37e -4	8.21e -4	6.36e -4	6.33e -4
$C14_{the,t_1}$	4.33e -4	6.50e -4	7.03e -4	6.88e -4	1.79e -4	1.07e -5	1.05e -5	1.02e -5	1.89e -4	2.43e -4	2.13e -4	2.79e -4
$C14_{act,t_2}$	0.003 1	3.65e -4	0.001 8	0.001 8	0.001 5	4.62e -5	3.22e -5	2.93e -5	0.004 2	0.004 3	0.003 2	0.002 4
$C14_{the,t_2}$	2.95e -4	5.53e -4	8.95e -4	7.95e -4	1.68e -4	1.40e -5	1.32e -5	1.25e -5	1.95e -4	1.95e -4	1.43e -4	3.57e -4
$C15_{act}$	0.032 1	0.002 0	0.057 4	0.060 9	0.015 1	3.75e -5	3.33e -5	3.05e -5	0.004 7	0.005 0	0.004 3	0.003 4
$C15_{the}$	3.50e -4	0.002 1	0.039 0	0.045 5	2.34e -4	2.56e -5	2.39e -5	2.10e -5	9.16e -5	1.01e -4	1.22e -4	2.72e -4

Notes. [Table 8](#) reports the mean magnitude of jumps (\overline{JM}) for both actual and theoretical BRIC Eurobond prices. \overline{JM} estimates are split into three groups: realized volatility, monthly range, and realized range estimates. All average values reported, are t-test significant in a 5% significance level.

Table 9.

Average ratio of magnitude of the jump component of risk to the magnitude of the continuous component (\overline{JR}).

	RV_t m	BPV_t m	$RV_{t,ma}$ $adj^{(1)}$	$RV_{t,ma}$ $adj^{(2)}$	$MR_{t,P}$ ar	MR_t GK	MR_t RS	MR_t YZ	$RR_{t,P}$ ar	RR_t GK	$RR_{t,R}$ S	$RR_{t,Y}$ Z
$B14_{act}$	0.48 04	10.4 8	0.7474	0.7474	0.700 7	1.43	1.24	1.29	1.08	1.14	1.33	0.51 61
$B14_{the}$	2.33	9.07	2.02	1.87	2.60	0.44 52	0	0	2.56	4.01	6.27	1.36
$B11_{act}$	1.52	5.04	0.8948	0.8788	0.684 9	1.73	1.76	1.55	1.02	8.21	5.02	1.22
$B11_{the}$	5.47	3.06	2.46	2.49	1.88	1.85	1.06	1.46	5.10	5.10	5.10	5.10
$B12_{act}$	1.84	7.51	0.4638	0.4261	0.797 4	0.95 87	0.90 84	1.27	1.65	1.83	1.43	1.69
$B12_{the}$	3.98 6	14.1 6	1.58	1.69	1.73	1.61	1.39	1.64	5.87	5.87	5.87	5.87
$R13_{act}$	1.22	16.3 3	0.4443	0.4688	1.62	0.75 31	0.65 38	0.52 43	0.67 94	0.71 49	1.11	0.57 93
$R13_{the}$	2.86	6.11	2.01	1.97	4.04	0.22 49	0	0	6.18	6.43	4.62	1.63
$R10_{act,t_1}$	0.86 22	22.2 5	1.03	1.06	2.25	1.83	1.61	1.72	7.91	32.9 3	26.6 1	32.5 9
$R10_{the,t_1}$	2.33	5.71	1.78	1.54	1.27	0.99 34	0.75 03	0.75 57	2.01	12.0 2	14.9 4	17.3
$R10_{act}$	1.42	15.5	0.8640	1.05	0.743	1.58	1.05	0.89	1.21	1.26	2.22	1.54

	RV_t^m	BPV_t^m	$RV_{t,ma}^a$ $d^{(1)}$	$RV_{t,ma}^a$ $d^{(2)}$	$MR_{t,P}^{an}$	MR_t^{GK}	MR_t^{RS}	MR_t^{YZ}	$RR_{t,P}^{an}$	RR_t^{GK}	$RR_{t,R}^S$	$RR_{t,Y}^Z$
ct_2		6			7			14				
$R10_{th}$ e_2	2.89	5.26	2.16	1.67	1.30	1.07	0.65 71	0.66 52	2.07	2.17	1.66	2.60
$I16_{act}$	1.22	7.38	1.14	1.14	0.858 9	2.63	18.0 0	16.5 1	2.47	1.03	1.06	1.27
$I16_{the}$	13.1 5	8.66	2.96	2.79	3.50	15.1 1	10.6 5	9.74	13.2 0	13.7 9	10.4 5	14.3 4
$C14_a$ ct_1	1.69	5.63	1.23	1.23	1.35	0.87 54	1.91	1.68	1.21	1.36	0.85 20	1.58
$C14_{th}$ e_1	2.12	8.71	0.7765	0.7739	0.877 1	0.28 45	0	0	1.18	1.38	1.73	0.67 20
$C14_a$ ct_2	8.02	5.32	3.64	3.61	4.50	10.7 8	7.51	6.85	14.7 0	15.2 7	11.2 8	7.21
$C14_a$ ct_2	0.73 41	7.95	1.09	0.9977	1.21	0.39 94	0	0	1.16	1.16	1.09	0.51 76
$C15_{act}$	53.2 6	16.0 6	2.06	2.18	32.92	2.93	10.7 6	9.84	4.00	4.16	2.73	3.65
$C15_{the}$	0.82 22	17.6 6	1.25	1.46	0.994 0	1.02	1.87	1.64	0.33 27	0.36 67	0	0.88 76

Notes. [Table 9](#) reports the average ratio of magnitude of the jump component of risk to the magnitude of the continuous component (\overline{JR}) for both actual and theoretical BRIC Eurobond prices. \overline{JR} estimates are split into three groups: realized volatility, monthly range, and realized range estimates. All average values reported, are t-test significant in a 5% significance level.

Table 10.

Average frequency of jump occurrence (\overline{J}).

	RV_t^m	BPV_t^m	$RV_{t,ma}^a$ $d^{(1)}$	$RV_{t,ma}^a$ $d^{(2)}$	$MR_{t,P}^{an}$	MR_t^{GK}	MR_t^{RS}	MR_t^{YZ}	$RR_{t,P}^{an}$	RR_t^{GK}	$RR_{t,R}^S$	$RR_{t,Y}^Z$
$B14_{act}$	0.41 67	0.91 67	0.5000 □	0.5000 □	0.333 3	0.22 22	0.16 67	0.13 89	0.27 78	0.30 56	0.22 22	0.41 67
$B14_{the}$	0.36 11	1.00 □	0.5556 □	0.5556 □	0.250 0	0.02 78	0.02 78	0.02 78	0.13 89	0.11 11	0.08 33	0.27 78
$B11_{act}$	0.38 89	0.77 78	0.8056 □	0.8056 □	0.444 4	0.41 67	0.33 33	0.33 33	0.41 67	0.66 67	0.25 00	0.77 78
$B11_{the}$	0.25 00	0.88 89	0.5000 □	0.5000 □	0.361 1	0.25 00	0.25 00	0.19 44	0.47 22	0.47 22	0.47 22	0.47 22
$B12_{act}$	0.36 11	0.86 11	0.6111 □	0.6389 □	0.361 1	0.50 00	0.33 33	0.25 00	0.63 89	0.52 78	0.41 67	0.88 89
$B12_{the}$	0.25 00	0.86 11	0.5556 □	0.5556 □	0.277 8	0.27 78	0.22 22	0.19 44	0.50 00	0.50 00	0.50 00	0.50 00
$R13_{act}$	0.33 33	0.94 44	0.4444	0.4722	0.611 1	0.33 33	0.16 67	0.16 67	0.30 56	0.22 22	0.19 44	0.69 44
$R13_{the}$	0.25 00	1.00 □	0.6389 □	0.6667 □	0.166 7	0.08 33	0.05 55	0.05 55	0.11 11	0.11 11	0.11 11	0.61 11

	RV_t^m	BPV_t^m	$RV_{t,ma}^a$ $d^{(1)}$	$RV_{t,ma}^a$ $d^{(2)}$	$MR_{t,P}^{a^h}$	MR_t^{GK}	MR_t^{RS}	MR_t^{YZ}	$RR_{t,P}^{a^h}$	RR_t^{GK}	$RR_{t,R}^S$	$RR_{t,Y}^Z$
$R10_a$	0.41	0.80	0.5833	0.5833	0.527	0.38	0.33	0.30	0.41	0.88	0.88	0.91
ct_1	67	56			8	89	33	56	67	89	89	67
$R10_{th}$	0.30	0.88	0.6944	0.7222	0.222	0.27	0.22	0.19	0.30	0.97	0.94	0.97
e_1	56	89			2	78	22	44	56	22	44	22
$R10_a$	0.44	0.69	0.5556	0.5556	0.500	0.58	0.52	0.52	0.72	0.75	0.50	0.91
ct_2	44	44			0	33	78	78	22	00	00	67
$R10_{th}$	0.27	0.91	0.6944	0.7222	0.222	0.22	0.19	0.16	0.44	0.44	0.33	0.63
e_2	78	67			2	22	44	67	44	44	33	89
$M6_{act}$	0.25	0.91	0.6111	0.6111	0.305	0.08	0.05	0.05	0.11	0.11	0.11	0.30
	00	67			6	33	56	56	11	11	11	56
$M6_{ne}$	0.19	0.97	0.5278	0.5278	0.333	0.02	0.02	0.02	0.11	0.11	0.08	0.16
	44	22			3	78	78	78	11	11	33	67
$C14_a$	0.36	1.00	0.7222	0.7222	0.250	0.05	0.02	0.02	0.33	0.22	0.16	0.72
ct_1	11				0	56	78	78	33	22	67	22
$C14_{th}$	0.13	1.00	0.7222	0.7500	0.333	0.02	0.02	0.02	0.22	0.16	0.11	0.63
e_1	89				3	78	78	78	22	67	11	89
$C14_a$	0.30	0.97	0.7500	0.7500	0.277	0.02	0.02	0.02	0.13	0.13	0.13	0.41
ct_2	56	22			8	78	78	78	89	89	89	67
$C14_a$	0.25	1.00	0.6667	0.6944	0.250	0.02	0.02	0.02	0.08	0.08	0.05	0.38
ct_2	00				0	78	78	78	33	33	56	89
$C15_{act}$	0.44	0.91	0.7222	0.7222	0.388	0.08	0.05	0.05	0.14	0.14	0.11	0.35
	44	67			9	33	56	56	29	29	11	71
$C15_{ne}$	0.19	1.00	0.6667	0.6667	0.277	0.05	0.02	0.02	0.08	0.08	0.08	0.16
	44				8	56	78	78	33	33	33	67

Notes. Table 10 reports the average frequency of jump occurrence (\bar{J}) for both actual and theoretical BRIC Eurobond prices. \bar{J} estimates are split into three groups: realized volatility, monthly range and realized range estimates. All average values reported, are t-test significant in a 5% significance level.

□

Indicates significance if the average frequency of jump occurrence (\bar{J}) is higher than 50%.

Table 11.

Theoretical vs actual prices.

	\bar{R}	\overline{SR}	\overline{JM}	\overline{JR}	\bar{J}
RV	60%	50%	63%	68%	43%
MR	85%	35%	25%	28%	5%
RR	55%	68%	55%	60%	15%

Notes. Table 11 reports the average percentage of bonds for which a risk or jump estimate (\bar{R} , \overline{SR} , \overline{JM} , \overline{JR} and \bar{J}) is higher for theoretical prices rather than for actual prices.

Table 12.

Summarized results for BRIC countries.

	\bar{R}	\overline{SR}	\overline{JM}	\overline{JR}	\bar{J}	J^*
<i>Brazil</i>	$BPV_{t,m}/MR_{t,YZ}$	$BPV_{t,m}/MR_{t,YZ}$	$RR_{t,GK}/MR_{t,YZ}$	$BPV_{t,m}/MR_{t,RS}$	$BPV_{t,m}/MR_{t,YZ}$	39%
<i>Russia</i>	$BPV_{t,m}/MR_{t,YZ}$	$MR_{t,YZ}/BPV_{t,m}$	$RR_{t,YZ}/MR_{t,YZ}$	$BPV_{t,m}/MR_{t,RS}$	$BPV_{t,m}/MR_{t,YZ}$	49%

	\bar{R}	\overline{SR}	\overline{JM}	\overline{JR}	\overline{J}	J^*
India	$BPV_{t,m} / MR_{t,YZ}$	$MR_{t,YZ} / BPV_{t,m}$	$RR_{t,YZ} / MR_{t,YZ}$	$MR_{t,RS} / RV_{t,ma}^{adj}$	$BPV_{t,m} / MR_{t,YZ}$	25%
China	$BPV_{t,m} / MR_{t,YZ}$	$MR_{t,YZ} / RR_{t,YZ}$	$RV_{t,ma}^{adj} / MR_{t,YZ}$	$BPV_{t,m} / MR_{t,GK}$	$BPV_{t,m} / MR_{t,YZ}$	28%

Notes. [Table 12](#) reports the estimators with the highest and (/) lowest values for the corresponding risk and jump measures (\bar{R} , \overline{SR} , \overline{JM} , \overline{JR} and \overline{J}). The last column provides the percentage of bonds (across estimators) for which the frequency of occurrence of significant jumps is higher than 50% (J^*).

Table 13.

Summarized results for groups of estimators.

	\bar{R}	\overline{SR}	\overline{JM}	\overline{JR}	\overline{J}
<i>RV</i>	China/Brazil	China/Brazil	China/Brazil	China/Brazil	Brazil/Russia
<i>MR</i>	Brazil/India	China/Russia	India/Russia	India/Russia	Russia/Russia
<i>RR</i>	China/Brazil	China/Brazil	India/Brazil	Russia/China	Russia/China

Notes. [Table 13](#) reports the countries with the highest and (/) lowest risk and jump measures for each group of estimators.

4.1. Unconditional distribution of return and volatility series

Many papers have examined the unconditional distribution of realized volatility (see [Illueca & Lafuente, 2006](#) and [Wang, Wu, & Yang, 2008](#)). [Table 4](#) provides summary statistics for the unconditional distribution of the realized volatilities. Volatility series for most of the BRIC Eurobonds and for most of volatility estimators are skewed to the right (skewness higher than zero) and leptokurtic (higher than three).

[Table 5](#) deploys results for normality testing. The normality (CVM and QQ) tests do reject the normality null hypothesis for most of the BRIC Eurobonds and across the board of estimators. The critical value derived under independence for the CVM-test is 0.458 (5%); and for the QQ-test is: 37.65 (5%). Most of volatilities (regardless either the group of estimators or the country they belong to) are not normally distributed. The null hypothesis of normality is not rejected for the $MR_{t,GK}$, $MR_{t,RS}$ and $MR_{t,YZ}$ estimators. All results for the skewness and kurtosis as well as for the normality testing of the unconditional distribution of volatilities are consistent for both actual and theoretical prices.

4.2. Risk

Risk is measured via the mean of magnitude of risk (\bar{R}) ([Table 6](#)) and the mean of Sharpe ratios (\overline{SR}) ([Table 7](#)).

4.2.1. Average magnitude of risk (\bar{R})

The realized volatility (*RV*) group of estimators has the highest mean magnitude of risk series (\bar{R}) across all BRIC countries. The highest (lowest) mean of risk (R_t) series (\bar{R}) comes from the $BPV_{t,m}$ ($MR_{t,YZ}$) estimator across BRIC Eurobonds, whereas the highest mean of risk (R_t) series (\bar{R}) comes from the Chinese Eurobonds across the board of estimators.

For the group of realized volatility estimators (RV) and the group of realized range-based volatility estimators (RR), Chinese (Brazilian) Eurobonds have the highest (lowest) mean magnitude of risk (R_t) series (\bar{R}) among BRIC countries. For the group of monthly ranges (MR), Brazilian (Indian) Eurobonds have the highest (lowest) \bar{R} among BRIC countries.

The $BPV_{t,m}$ ($RV_{t,ma\ adj^2}$) estimator has the highest (lowest) mean magnitude of risk (R_t) series (\bar{R}) among the realized volatility estimators (RV), across all BRIC Eurobonds. The $MR_{t,YZ}$ ($MR_{t,Par}$) estimator has the highest (lowest) \bar{R} among the monthly ranges (MR), across all BRIC Eurobonds. The $RR_{t,RS}$ ($RR_{t,YZ}$) estimator has the highest (lowest) \bar{R} among the realized range-based volatility estimators (RR), across all BRIC Eurobonds. Regarding the performance of risk estimators, via the mean magnitude of risk (R_t) series (\bar{R}), results are consistent across all BRIC Eurobonds. All mean values of risk estimates for all bonds and estimators are t-test statistically significant.

Moreover, the mean magnitude of risk (R_t) series (\bar{R}) coming from theoretical prices (theoretical-price risk) is higher than the mean risk coming from actual market prices (actual-price risk). This result is evident in most of estimators and BRIC bonds. Across most of the eurobonds, the higher the expiry period, the higher the mean magnitude of risk (\bar{R}) is.

4.2.2. Average Sharpe ratio (\bar{SR})

The monthly range group of estimators (MR) has the highest mean of Sharpe ratios (SR_t) series (\bar{SR}) across all BRIC countries. The highest (lowest) \bar{SR} comes from the $MR_{t,YZ}$ ($BPV_{t,m}$) estimator across BRIC Eurobonds, whereas the highest (lowest) \bar{SR} comes from the Chinese (Brazilian) Eurobond across the board of estimators.

In specific, regarding Brazil, the RV realized volatility (MR monthly range) group of estimators has the highest (lowest) mean of Sharpe ratios (SR_t) series (\bar{SR}) among groups, and the $BPV_{t,m}$ ($MR_{t,YZ}$) estimator among individual estimators. Regarding Russia, the MR monthly range (RV realized volatility) group of estimators has the highest (lowest) \bar{SR} among groups, and the $MR_{t,YZ}$ ($BPV_{t,m}$) estimator among individual estimators. Regarding India, the MR monthly range (RV realized volatility) group of estimators has the highest (lowest) \bar{SR} among groups, and the $MR_{t,YZ}$ ($BPV_{t,m}$) estimator among individual estimators. Regarding China, the MR monthly range (RR realized range) group of estimators has the highest (lowest) \bar{SR} among groups, and the $MR_{t,YZ}$ ($RR_{t,YZ}$) estimator among individual estimators.

For all three (RV , MR and RR) groups of estimators, Chinese (Brazilian) Eurobonds have the highest (lowest) mean of Sharpe ratios (SR_t) series (\bar{SR}) among BRIC countries. The $BPV_{t,m}$ ($RV_{t,ma\ adj^2}$) estimator has the highest (lowest) mean of Sharpe ratios (SR_t) series (\bar{SR}) among the realized volatility estimators, across all BRIC Eurobonds. The $MR_{t,Par}$ ($MR_{t,YZ}$) estimator has the highest (lowest) \bar{SR} among the monthly ranges, across all BRIC Eurobonds. The $RR_{t,RS}$ ($RR_{t,GK}$) estimator has the highest (lowest) \bar{SR} among the realized range-based volatility estimators, across all BRIC Eurobonds.

Regarding the mean of Sharpe ratios (SR_t) series (\bar{SR}), all estimators are consistent and results change because of the informational content of BRIC bonds. All mean values of risk

estimates for all bonds and estimators are t-test statistically significant. Moreover, the mean of Sharpe ratios (SR_t) series (\overline{SR}) coming from theoretical prices (theoretical-price Sharpe ratios) is higher than the mean Sharpe ratio coming from actual market prices (actual-price Sharpe ratio). This result is evident in most of estimators and BRIC bonds. Across most of the eurobonds, the higher the expiry period, the higher the mean magnitude of Sharpe ratios (SR_t) series (\overline{SR}) is.

4.3. Jumps

[Eraker, Johannes, and Polson \(2003\)](#) as well as more recently [Atak and Kapetanios \(2013\)](#) provide results of significant average frequencies of occurrence (jump times) and significant magnitudes of jumps (jump sizes). [Barndorff-Nielsen and Shephard \(2006\)](#) signify the importance of jumps in asset prices compared to continuous sample paths, whereas [Todorov and Tauchen \(2011\)](#) suggest that volatility is a pure jump process with jumps of infinite variation. In the present paper, the significance of jumps is measured via the mean magnitude of jumps (\overline{JM}) ([Table 8](#)), the ratio of the mean magnitude of the jump component of risk to the mean magnitude of the continuous component of risk (\overline{JR})¹⁰ ([Table 9](#)) and the average frequency of jump occurrence (\overline{J})¹¹ ([Table 10](#)).

4.3.1. Average magnitude of jumps (\overline{JM})

The *RR* realized range (*MR* monthly range) group of estimators has the highest (lowest) mean magnitude of jumps (\overline{JM}) series across all BRIC countries. The highest (lowest) \overline{JM} series comes from the $RR_{tYZ}(MR_{tYZ})$ estimator across BRIC Eurobonds, whereas the highest (lowest) \overline{JM} comes from the Indian (Brazilian) Eurobond across the board of estimators.

In specific, regarding Brazil, the *RR* realized range (*MR* monthly range) group of estimators has the highest (lowest) mean magnitude of jumps (JM_t) series (\overline{JM}) among groups, and the $RR_{tGK}(MR_{tYZ})$ estimator among individual estimators. Regarding Russia and India, the *RR* realized range (*RV* realized volatility) group of estimators has the highest (lowest) \overline{JM} among groups, and the $RR_{tYZ}(MR_{tYZ})$ estimator among individual estimators. Regarding China, the *RV* realized volatility (*MR* monthly range) group of estimators has the highest (lowest) \overline{JM} among groups, and the $RV_{tma\ adj}^{(1)}(MR_{tYZ})$ estimator among individual estimators.

For the group of realized volatility estimators, Indian (Brazilian) Eurobonds have the highest (lowest) mean magnitude of jumps (JM_t) series (\overline{JM}) among BRIC countries. For the group of monthly ranges, Indian (Russian) Eurobonds have the highest (lowest) \overline{JM} among BRIC countries. For the group of realized range-based volatility estimators, Indian (Brazilian) Eurobonds have the highest (lowest) \overline{JM} among BRIC countries.

The $RV_{tma\ adj}^{(1)}(BPV_{tm})$ estimator has the highest (lowest) mean magnitude of jumps (JM_t) series (\overline{JM}) among the realized volatility estimators, across all BRIC Eurobonds. The $MR_{tPar}(MR_{tYZ})$ estimator has the highest (lowest) \overline{JM} among the monthly ranges,

across all BRIC Eurobonds. The $RR^{(YZ)}$ ($RR^{(RS)}$) estimator has the highest (lowest) \overline{JM} among the realized range-based volatility estimators, across all BRIC Eurobonds. Regarding the mean magnitude of jumps (JM_t) series (\overline{JM}), all estimators are consistent and results change because of the informational content of BRIC bonds. All mean values of jump magnitude estimates for all bonds and estimators are t-test statistically significant. Moreover, the mean magnitude of jumps (JM_t) series (\overline{JM}) coming from theoretical prices (theoretical-price Jump magnitudes) is higher than the mean magnitude of jumps coming from actual market prices (actual-price Jump magnitudes). This result is evident in most of estimators and BRIC bonds. Across most of the eurobonds, the higher the expiry period, the higher the mean magnitude of jumps (JM_t) series (\overline{JM}) is.

4.3.2. Average magnitude of jump component of risk relative to the magnitude of the continuous component (\overline{JR})

The RV realized volatility (MR monthly range) group of estimators has the highest (lowest) mean (JR_t) series (\overline{JR}) across all BRIC countries. The highest (lowest) \overline{JR} comes from the $BPV^{(m)}$ ($MR^{(RS)}$) estimator across BRIC Eurobonds, whereas the highest (lowest) \overline{JR} comes from the Chinese (Brazilian) Eurobond across the board of estimators.

In specific, regarding Brazil and Russia, the RV realized volatility (MR monthly range) group of estimators has the highest (lowest) mean of JR_t series (\overline{JR}) among groups, and the $BPV^{(m)}$ ($MR^{(RS)}$) estimator among individual estimators. Regarding India, the MR monthly range (RV realized volatility) group of estimators has the highest (lowest) \overline{JR} among groups, and the $MR^{(RS)}$ ($RV^{(ma\ adj^1)}$) estimator among individual estimators. Regarding China, the RV realized volatility (MR monthly range) group of estimators has the highest (lowest) \overline{JR} among groups, and the $BPV^{(m)}$ ($MR^{(GK)}$) estimator among individual estimators.

For the group of RV realized volatility estimators and the group of RR realized range estimators, Chinese (Brazilian) Eurobonds have the highest mean of JR_t series (\overline{JR}) among BRIC countries. For the group of MR monthly ranges, Indian (Russian) Eurobonds have the highest (lowest) \overline{JR} among BRIC countries.

The $BPV^{(m)}$ ($RV^{(ma\ adj^2)}$) estimator has the highest mean of JR_t series (\overline{JR}) among the realized volatility estimators, across all BRIC Eurobonds. The $MR^{(Pa)}$ ($MR^{(RS)}$) estimator has the highest (lowest) \overline{JR} among the monthly ranges, across all BRIC Eurobonds. The $RR^{(GK)}$ ($RR^{(Pa)}$) estimator has the highest (lowest) \overline{JR} among the realized range-based volatility estimators, across all BRIC Eurobonds.

Regarding the mean of JR_t series (\overline{JR}), all estimators are consistent and results change because of the informational content of BRIC bonds. All mean ratios for all bonds and estimators are t-test statistically significant. Moreover, the mean of JR_t series (\overline{JR}) coming from theoretical prices (theoretical-price Jump ratio) is higher than the mean Jump ratio coming from actual market prices (actual-price Jump ratio). This result is evident in most of estimators and BRIC bonds. Across most of the eurobonds, the shorter the expiry period, the higher the mean of JR_t series (\overline{JR}) is.

4.3.3. Average frequency of jump occurrences (\bar{J})

The RV realized volatility (MR monthly range) group of estimators has the highest (lowest) average frequency of jump occurrence (J_t) series (\bar{J}) across all BRIC countries. The highest (lowest) \bar{J} comes from the BPV_{tm} (MR_{YZ}) estimator across BRIC Eurobonds, whereas the highest (lowest) \bar{J} comes from the Brazilian (Russian) Eurobond across the board of estimators.

For all BRIC countries, the RV realized volatility (MR monthly range) group of estimators has the highest (lowest) average frequency of jump occurrence series (\bar{J}) among groups, and the BPV_{tm} (MR_{YZ}) estimator among individual estimators.

For the group of RV realized volatility estimators and the group of MR monthly ranges, Brazilian (Russian) Eurobonds have the highest average frequency of jump occurrence series (\bar{J}) among BRIC countries. For the group of RR realized range-based volatility estimators, Russian (Chinese) Eurobonds have the highest \bar{J} among BRIC countries.

The BPV_{tm} (RV_{tm}) estimator has the highest (lowest) average frequency of jump occurrence (\bar{J}) among the RV realized volatility estimators, across all BRIC Eurobonds. The MR_{Pa} (MR_{YZ}) estimator has the highest (lowest) \bar{J} among the MR monthly ranges, across all BRIC Eurobonds. The RR_{YZ} (RR_{RS}) estimator has the highest (lowest) (\bar{J}) among the RR realized range-based volatility estimators, across all BRIC Eurobonds.

Regarding the mean frequency of jump occurrence (J_t) series (\bar{J}), all estimators are consistent and results change because of the informational content of BRIC bonds. All mean values of jump magnitude estimates for all bonds and estimators are t-test statistically significant. Moreover, the mean frequency of jump occurrence (J_t) series (\bar{J}) coming from theoretical prices (theoretical-price Jump frequency) is higher than the mean frequency of jumps coming from actual market prices (actual-price Jump frequencies). This result is evident in most of estimators and BRIC bonds. Across most of the eurobonds, the higher the expiry period, the higher the mean frequency of jump occurrence (J_t) series (\bar{J}) is.

Regarding the frequency of jump occurrence, Russian (Indian) Eurobonds have the highest (lowest) number of estimators for which the \bar{J} is significant¹². The RV realized volatility (MR monthly range) group of estimators has the highest (lowest) number of Eurobonds for which the \bar{J} is significant. The BPV_{tm} (MR_{YZ}) estimator has the highest (lowest) number of Eurobonds for which the \bar{J} is significant.

5. Conclusions

Concluding remarks concern results across all significance-measures: two risk significance-measures (\bar{R} , and \bar{SR}) and three jump significance-measures (\bar{JM} , \bar{JR} and \bar{J}). The overall significance is evident when most of the significance measures are significant. The significance of each either risk- or jump-measure is indicated as reported in the empirical findings section. Firstly, findings are consistent as far as there are not many differences between the group of the two risk measures and the group of the three jump measures.

Moreover, there are not many differences among the two risk measures and also among the three jump measures. Moreover, all risk and jump measures from theoretical prices are higher than those from actual prices, across bonds and estimators. Across most of the eurobonds and measures, the higher the expiry period, the higher is the significance of risk and jumps. This result is consistent with bond theory. The Chinese Eurobonds are the most significant, across the board of estimators. Among BRIC Eurobonds, the $C15_{the}$ Eurobond is the most significant.

The RV realized volatility group of estimators and the MR monthly range group of estimators are the most significant (in terms of both risk and jumps) across all BRIC countries. The most significant estimators are $BPV_{(t,m)}$ bipower variation (high in risk and jumps) and $MR_{(Y,Z)}$ monthly Yang & Zhang range (low in risk and jumps) across BRIC Eurobonds. All risk and jump significance-measures are consistent across the boards of estimators and BRIC Eurobonds.

For all BRIC countries, the RV realized volatility (MR monthly range) group of estimators retrieves the highest (lowest) estimates of risk and jumps. The bipower variation (monthly Yang & Zhang range) estimator produce the highest (lowest) estimates of risk and jumps.

For the RV realized volatility group and the RR realized range group of estimators, the Chinese (Brazilian) Eurobonds have the highest (lowest) estimates of risk and jumps among all BRIC Eurobonds (countries). For the group of MR monthly ranges, Brazilian (Russian) Eurobonds (Brazil) have the highest (lowest) estimates of risk and jumps among all BRIC Eurobonds (countries). Risk and jump estimates are higher (lower) for theoretical prices rather than actual prices for the RV realized volatility (MR monthly range) group of estimators. The present paper suggests that theoretical prices are better to be used instead of the actual. This empirical implication may trigger research on incorporating the theoretical pricing of Eurobonds into modeling, forecasting and investing Eurobonds. As BRICs (Brazil, Russia, India and China) become much larger force in the world economy, the accurate measurement and the properties of BRIC Eurobonds risk will become more important in the international financial markets and academia. The direct implications concern pricing structured products, fund management, the predictability of risk, and international asset allocation.

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Corresponding author. Tel.: + 44 1522 835634.

1

Tel.: + 44 1522 835612.

2

This acronym refers to the association of Brazil, Russia, India and China that first convened in June 2009 ostensibly in response to the fallout of the 2008–09 financial crisis. In reality, it was formed to offer an alternative framework of global governance anchored by the leading emerging economies (see, [Goodliffe & Sberro, 2012](#)).

3

Eurobonds are issued offshore, in a currency different from that of the market where the bond is arranged. The increased role of Eurobonds was signified by [Henderson, Jegadeesh, and Weisbach \(2006\)](#), among others.

4

The recent financial crisis period had an international impact from February 2007 up to February 2010. This is the target period of the present study.

5

[Zhang, Mykland, and Ait-Sahalia \(2005\)](#) showed that, in the presence of jumps, two-scales realized volatility (TSRV) estimates the integrated variance plus the sum of squared intraday jumps. A more recent analytical study is [Zhang \(2011\)](#).

6

[Jacquier and Okou \(2014\)](#) is a recent study in jumps in monthly realized volatility series.

7

More recent studies on the empirical applications, the properties of this detection scheme, the properties of jumps series are [Ait-Sahalia and Jacod \(2011\)](#), [Ait-Sahalia et al. \(2012\)](#), and [Ait-Sahalia, Fan, and Li \(2013\)](#).

8

These ratings were published on 12/31/2010. The Moody's ratings start from BB – (the worst rating) to the A+(best rating) in the following order: BB –, BB, BB +, BBB –, BBB, BBB +, A –, A, A +.

9

The asymptotic properties for their jump detection scheme were provided by [Barndorff-Nielsen and Shephard \(2006\)](#) and [Andersen et al. \(2010\)](#) as well.

10

Significance is indicated if the mean magnitude of the jump component of risk relative to the magnitude of the continuous component ($\bar{J}\bar{R}$) is higher than 1.

11

Significance is indicated if the average frequency of occurrence of jumps (\bar{J}) is higher than 50%.

12

Significance is indicated if the average frequency of jump occurrences (\bar{J}) is higher than 50%.

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